

# **Torus oscillations and the 17 minute QPO**

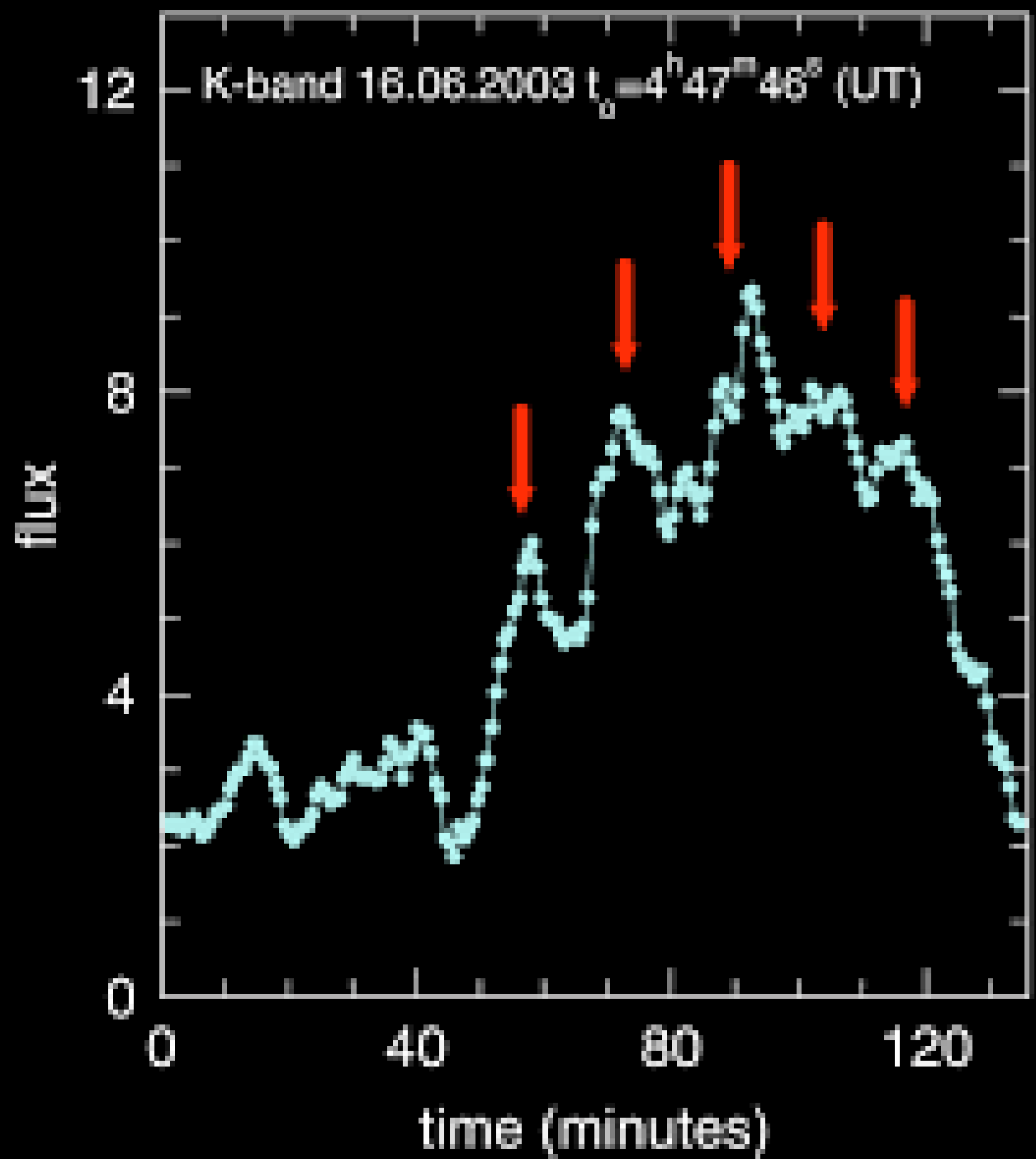
**(IR flares in Sgr A\*)**

**Włodek Kluźniak**  
**Copernicus Astronomical Center**

Aspen 2016.02.09

Sgr A\*  
Genzel et al 2003

17m QPO

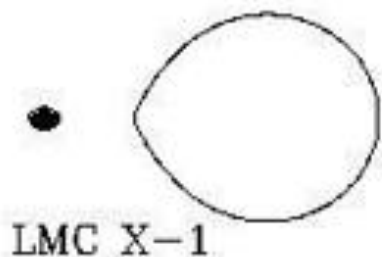


# Appearance of black hole and disk (light-bending)

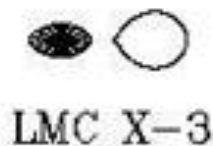
J.-A. Marck



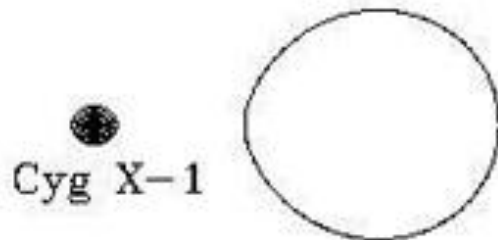

 Sun ←-----→ Mercury



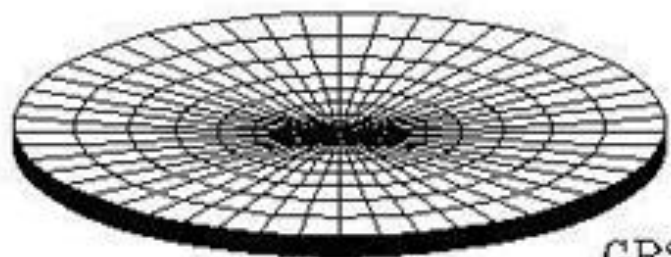
LMC X-1



LMC X-3



Cyg X-1



GRS 1915+105



XTE J1118+480 XTE J1859+226



GRS 1009-45 GRS 1124-683

SAX J1819.3-2525

GS 2000+25 H1705-250



GRO J1655-40

A0620-00 GRO J0422+32



4U 1543-47



GS 2023+338

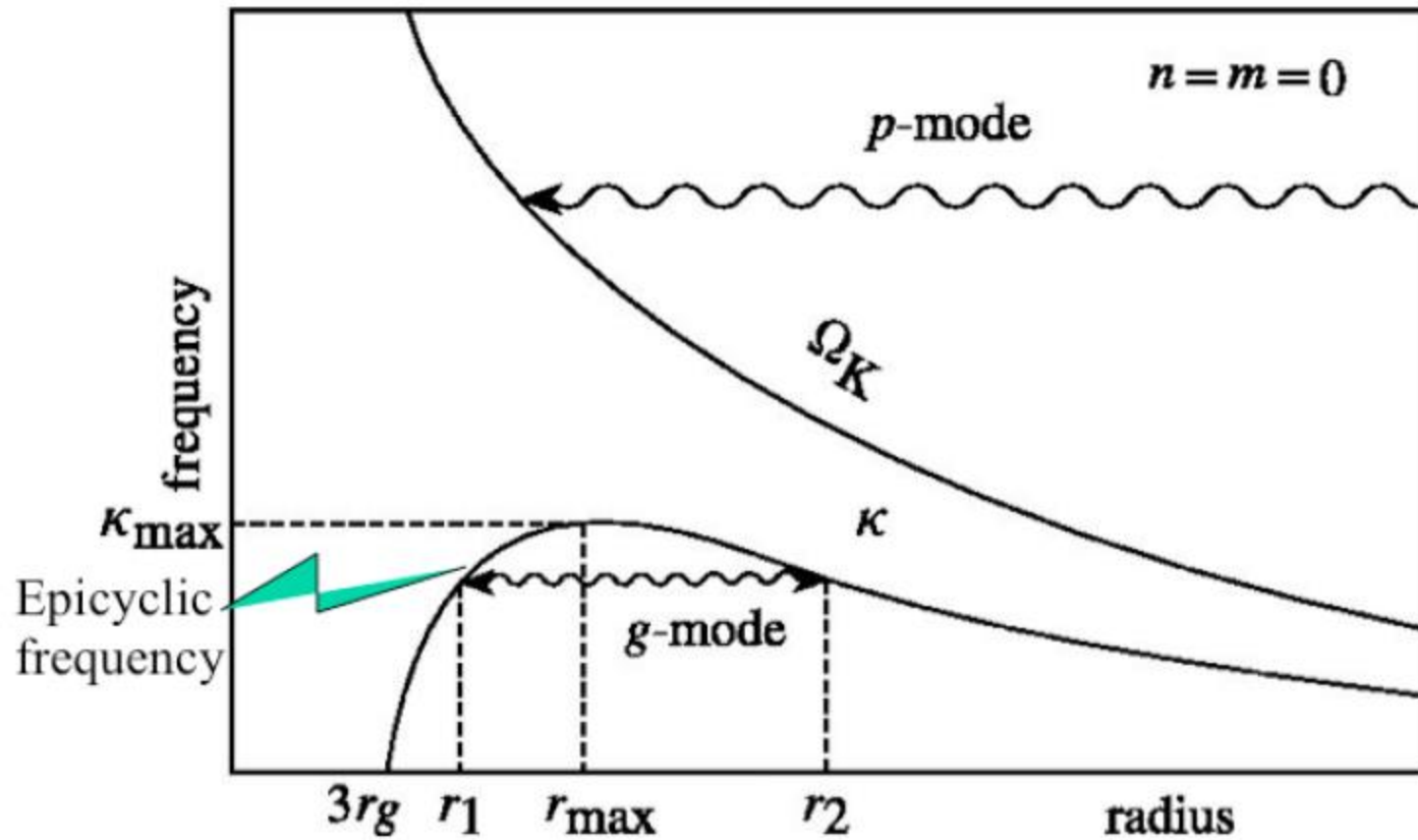


XTE J1550-564

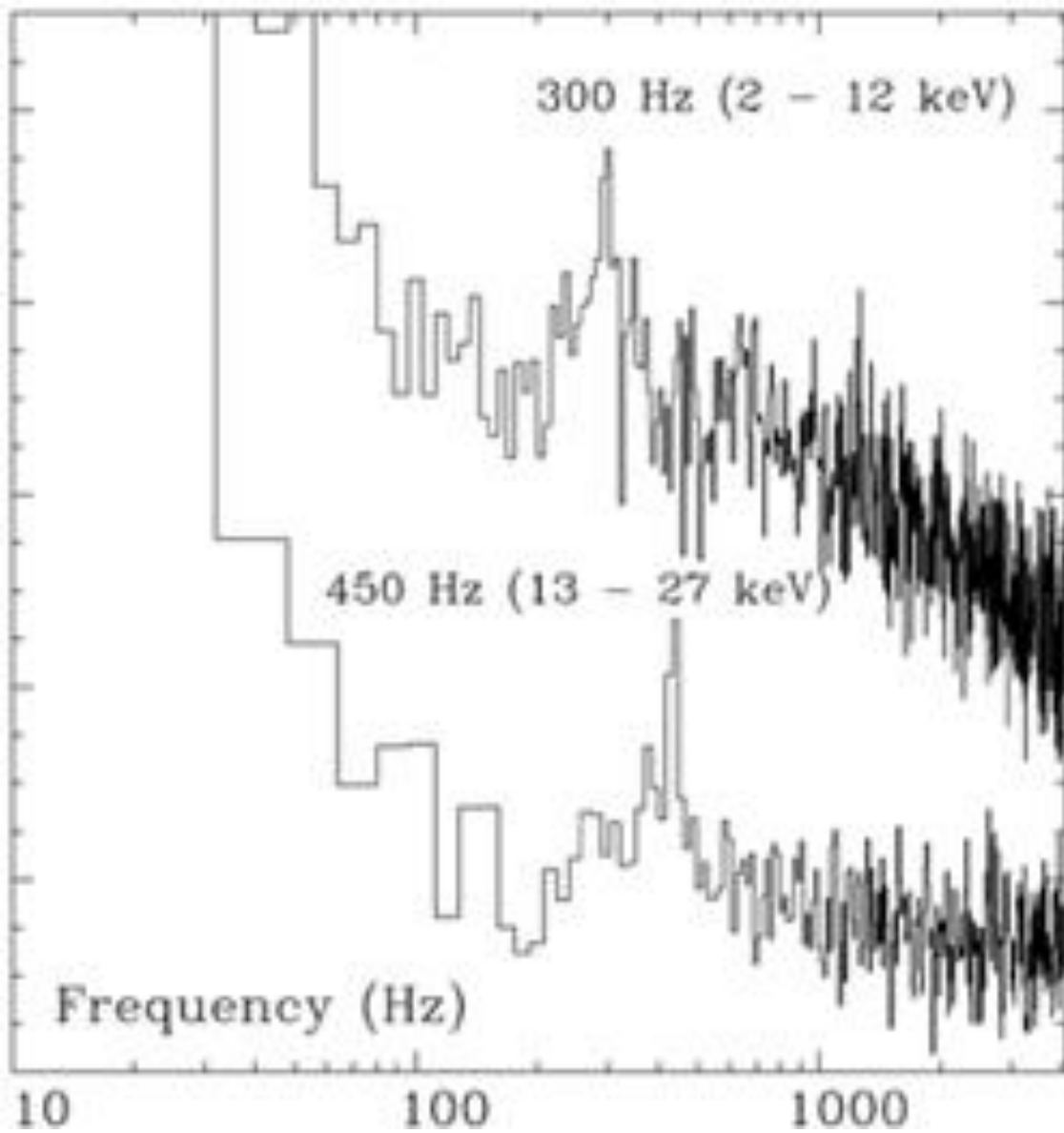
Size of BH binaries

J. Orosz

Okazaki, Atsuo T.; Kato, Shoji; Fukue, Jun: PASJ 39 (1987) 457  
Global trapped oscillations of relativistic accretion disks



Kato 2001  $\Downarrow \Rightarrow$  Diskoseismology of Nowak & Wagoner 16



Black hole  
GRO J 1655-40

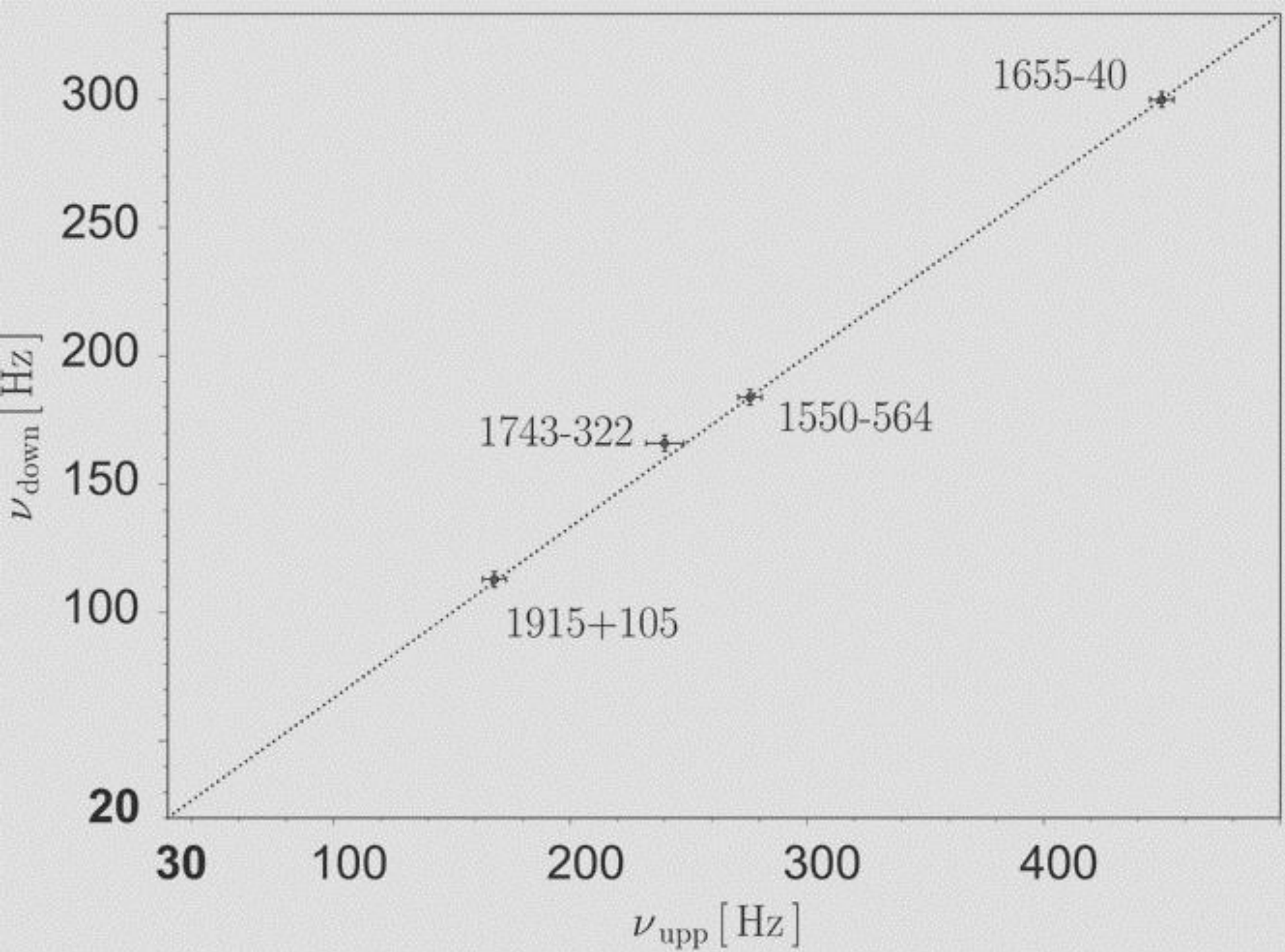
Strohmayer et al 2001

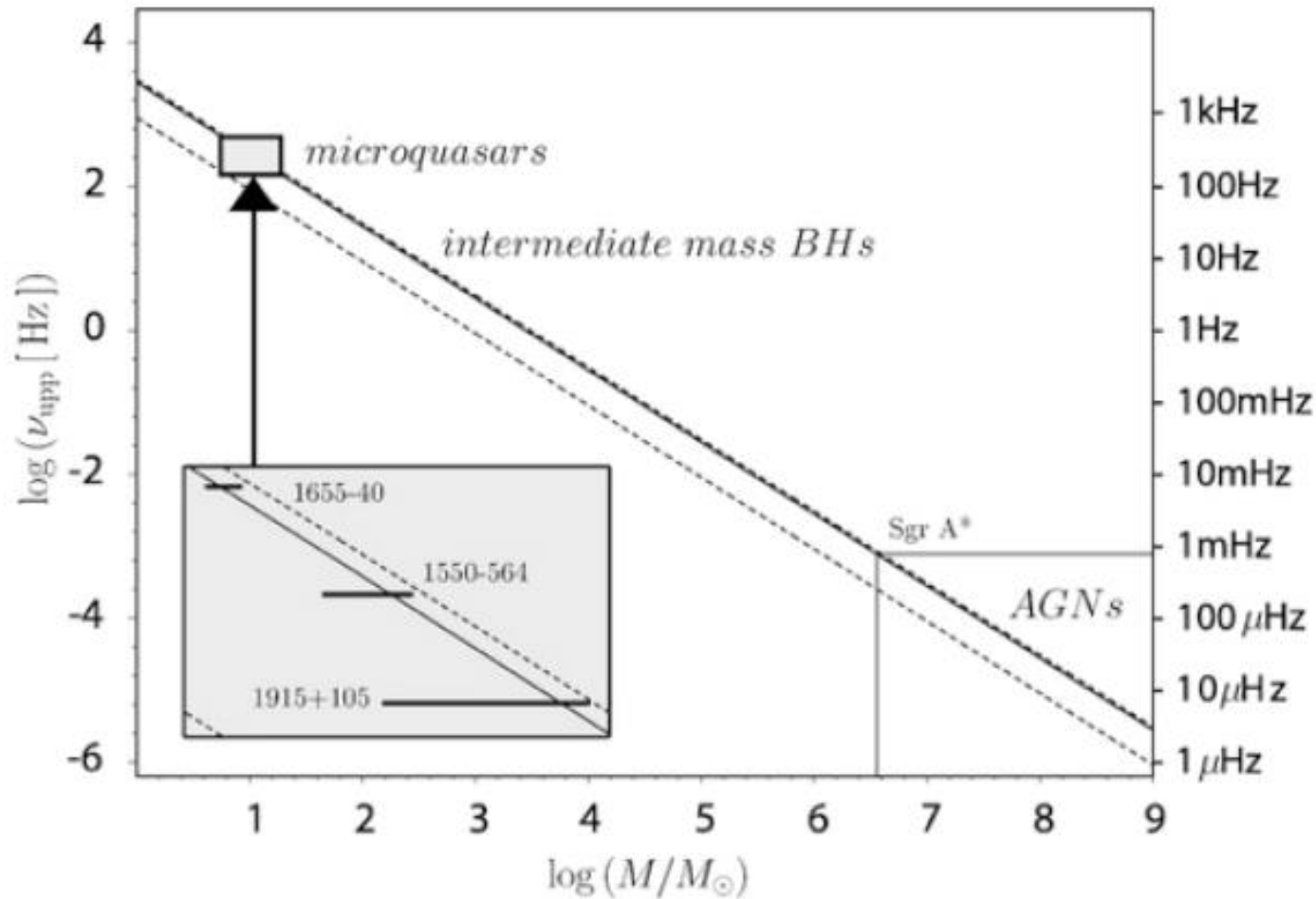
$450:300=3:2$

Kluźniak & Abramowicz  
2001

Twin high-frequency  
quasi-periodic oscillations  
HF QPOs

X-ray observations





In GR,  $f \sim 1/M$



Parametric resonance:

Mathieu eq.

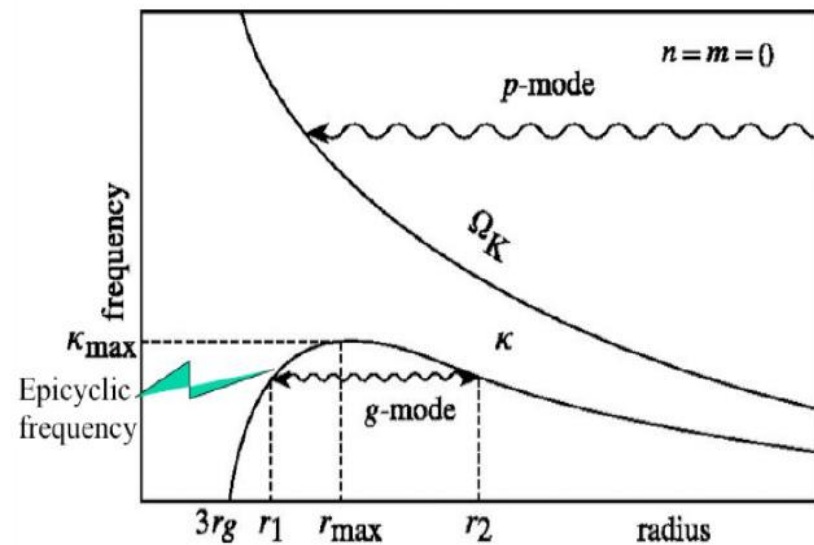
$$\ddot{U} + \omega_0^2[1 + h \cos(\omega_1 t)] U = 0$$

e.g., WK 2005

Resonance condition:  $\omega_0 = (n/2) \omega_1$ ,  $n = 1, 2, 3, \dots$

Suppose  $\omega_1 < \omega_0$  (as true for epicyclic frequencies),

then first possibility  $n=3 \Rightarrow 3:2$  ratio.



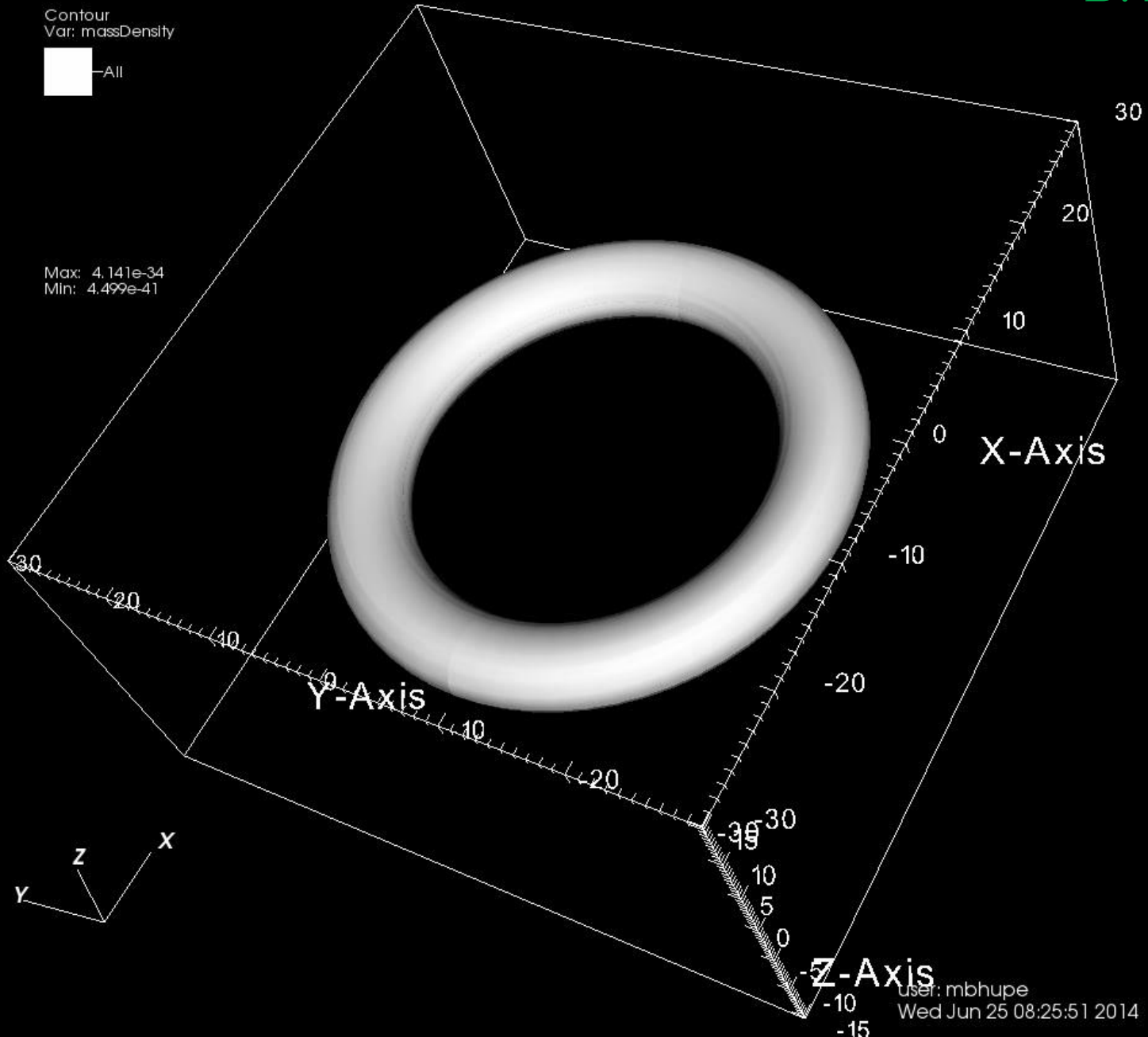
DB: out-Master.cosmos++  
Cycle: 0 Time:0

B. Mishra

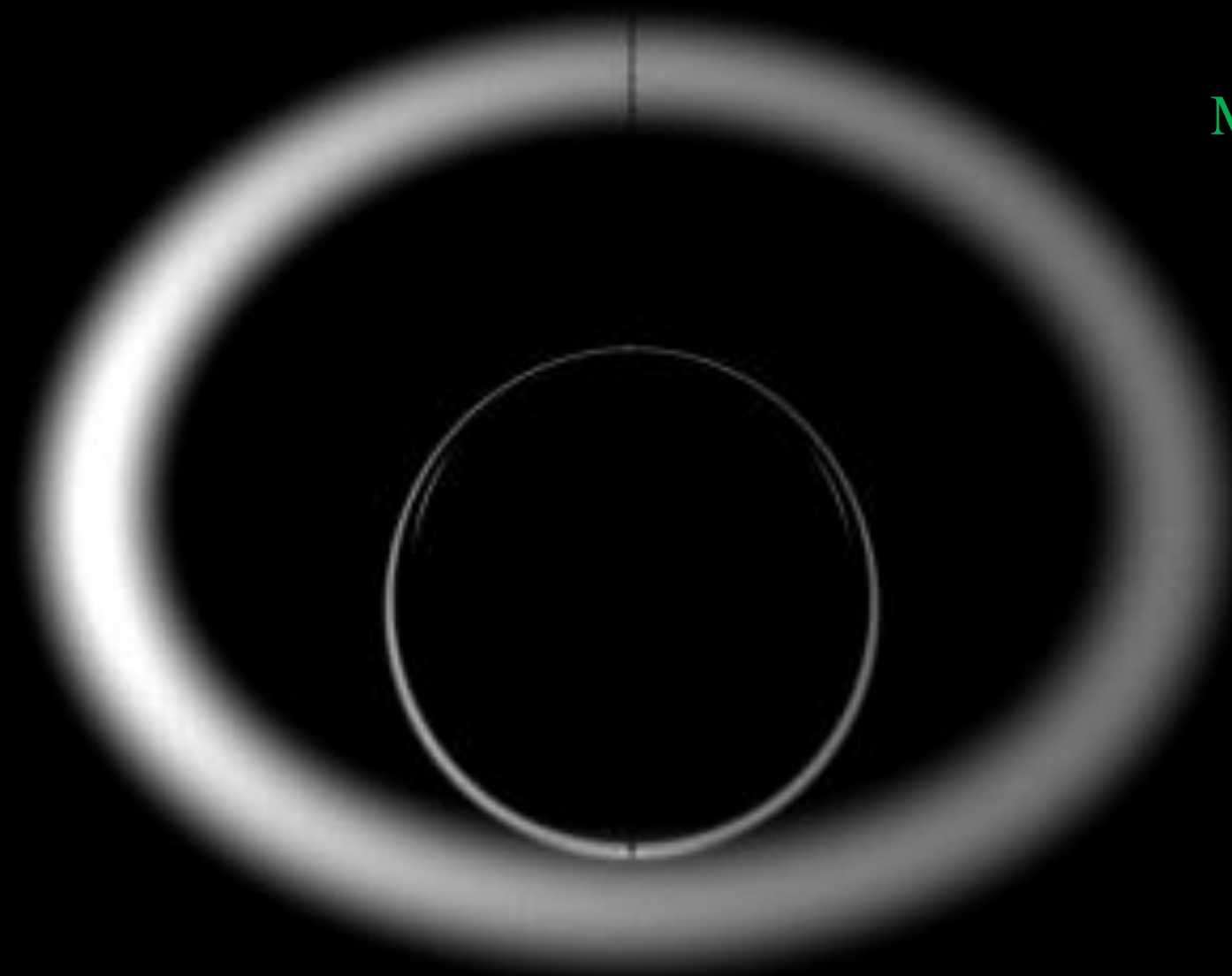
Contour  
Var: massDensity



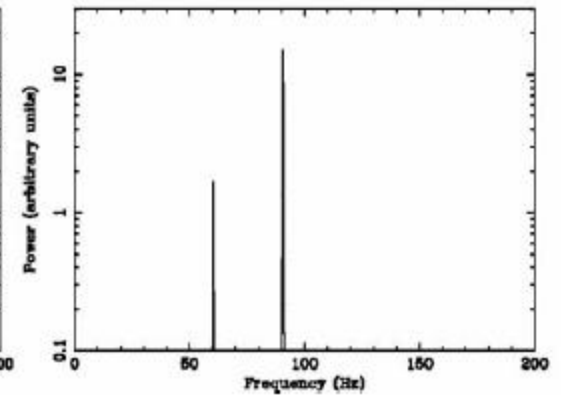
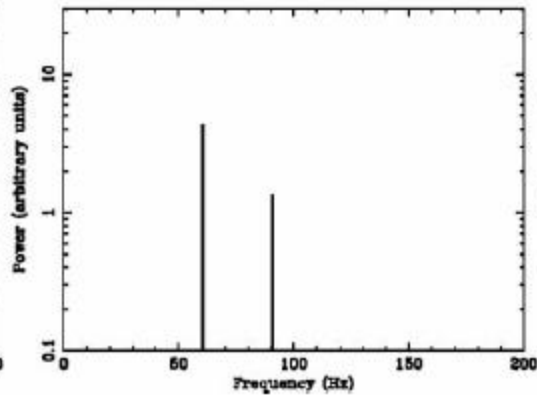
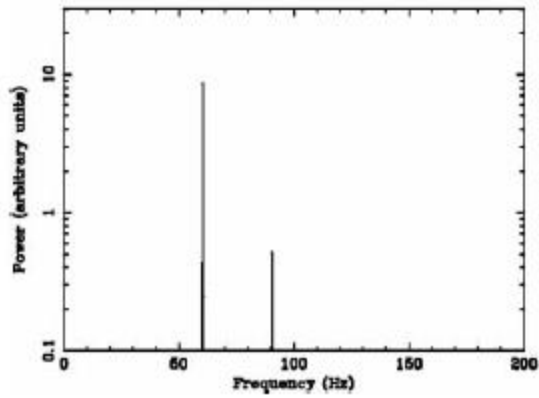
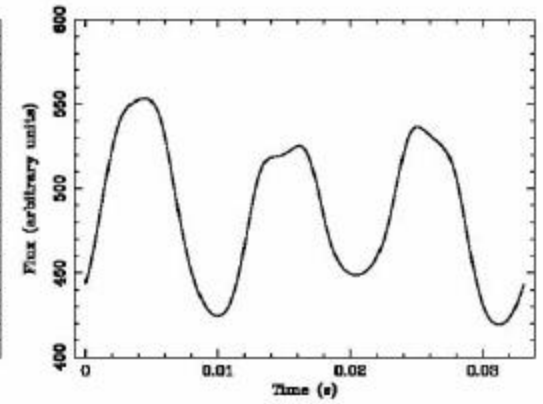
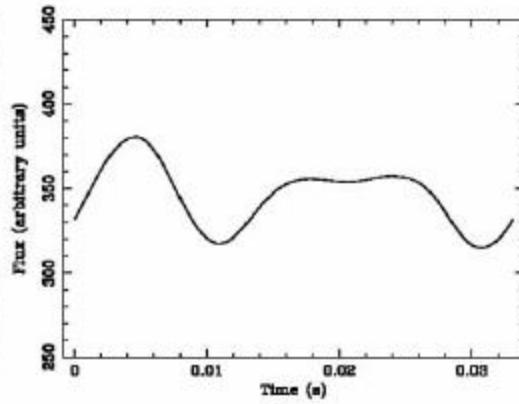
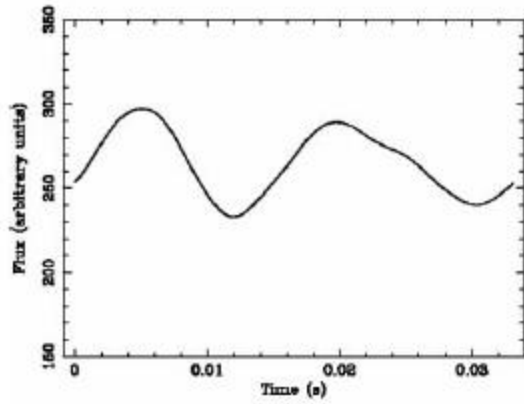
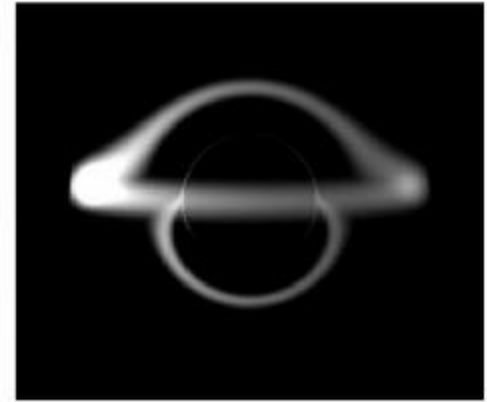
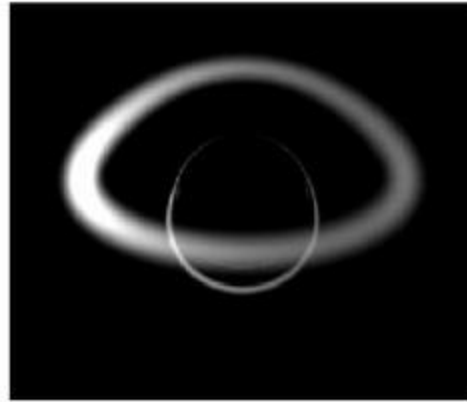
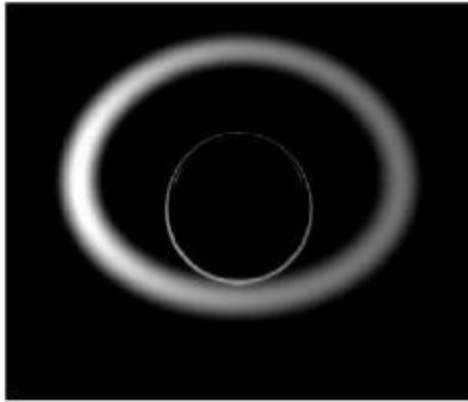
Max: 4.141e-34  
Min: 4.499e-41

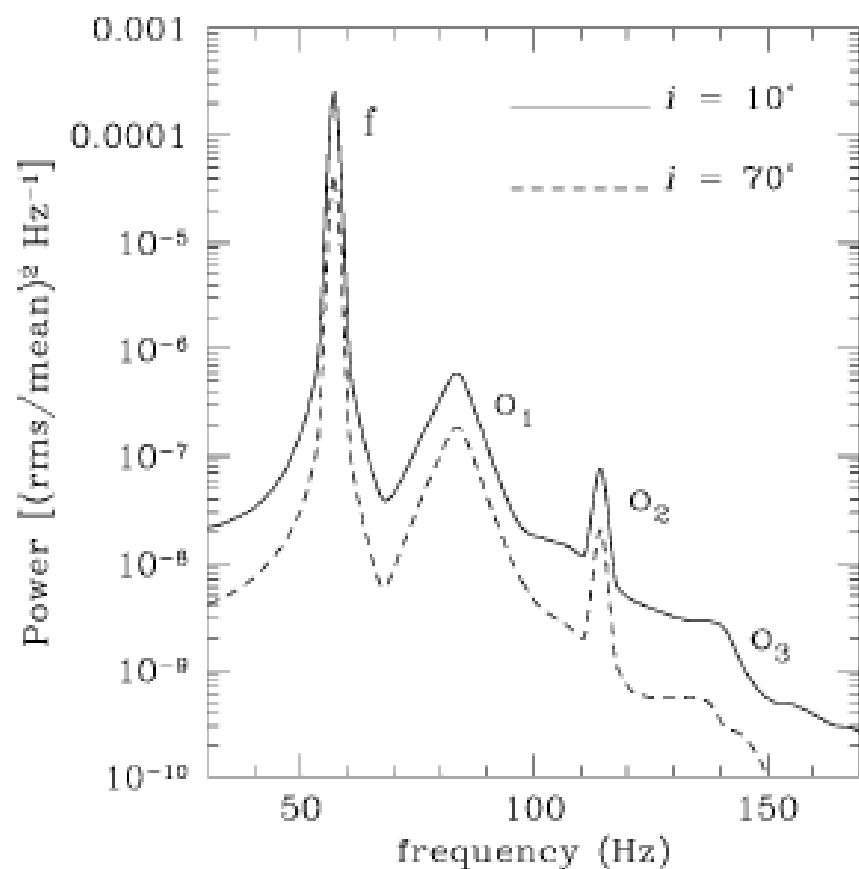


M. Bursa



# Bursa et al. 2004





## 4. DISCUSSION AND CONCLUSIONS

We have demonstrated a positive correlation between the intrinsic normal-mode oscillations of a pressure-supported torus and the extrinsic X-ray light curves and power spectra as seen by a distant observer. In addition to this being the first ray-tracing calculation exploiting dynamically the results of relativistic hydrodynamics simulations, our investigation confirms the feasibility of the oscillating-torus model as an explanation for the integer ratios seen in high-frequency QPO peaks. The specific parameters of the torus model still require further investigation in order to best fit the QPO data, including a more comprehensive study of black hole mass, spin, and inclination angles.

For the line emission models considered, the variation in the light curve is caused largely by the gravitational redshift of photons coming from different radii as the torus moves in and out of the black hole's potential well. Unlike the relativistic hot-spot model, for the same emission mechanism the oscillating-torus model predicts higher amplitude variations in the light curve for smaller inclination angles, while at higher angles the special relativistic beaming and gravitational lensing counter the gravitational redshift, reducing the variations in flux. On the other hand, the thermal emission model predicts

## EPICYCLIC OSCILLATIONS OF FLUID BODIES: NEWTONIAN NONSLENDER TORUS

OMER M. BLAES,<sup>1</sup> EVA ŠRÁMKOVÁ,<sup>2</sup> MAREK A. ABRAMOWICZ,<sup>2,3,4</sup> WŁODEK KLUŻNIAK,<sup>4,5</sup> AND ULF TORKELSSON<sup>3</sup>

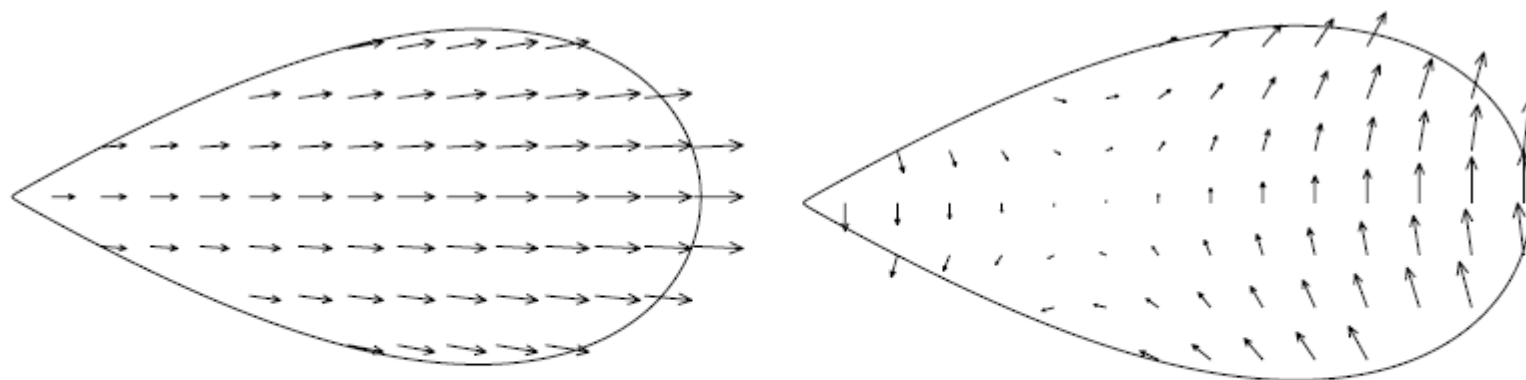
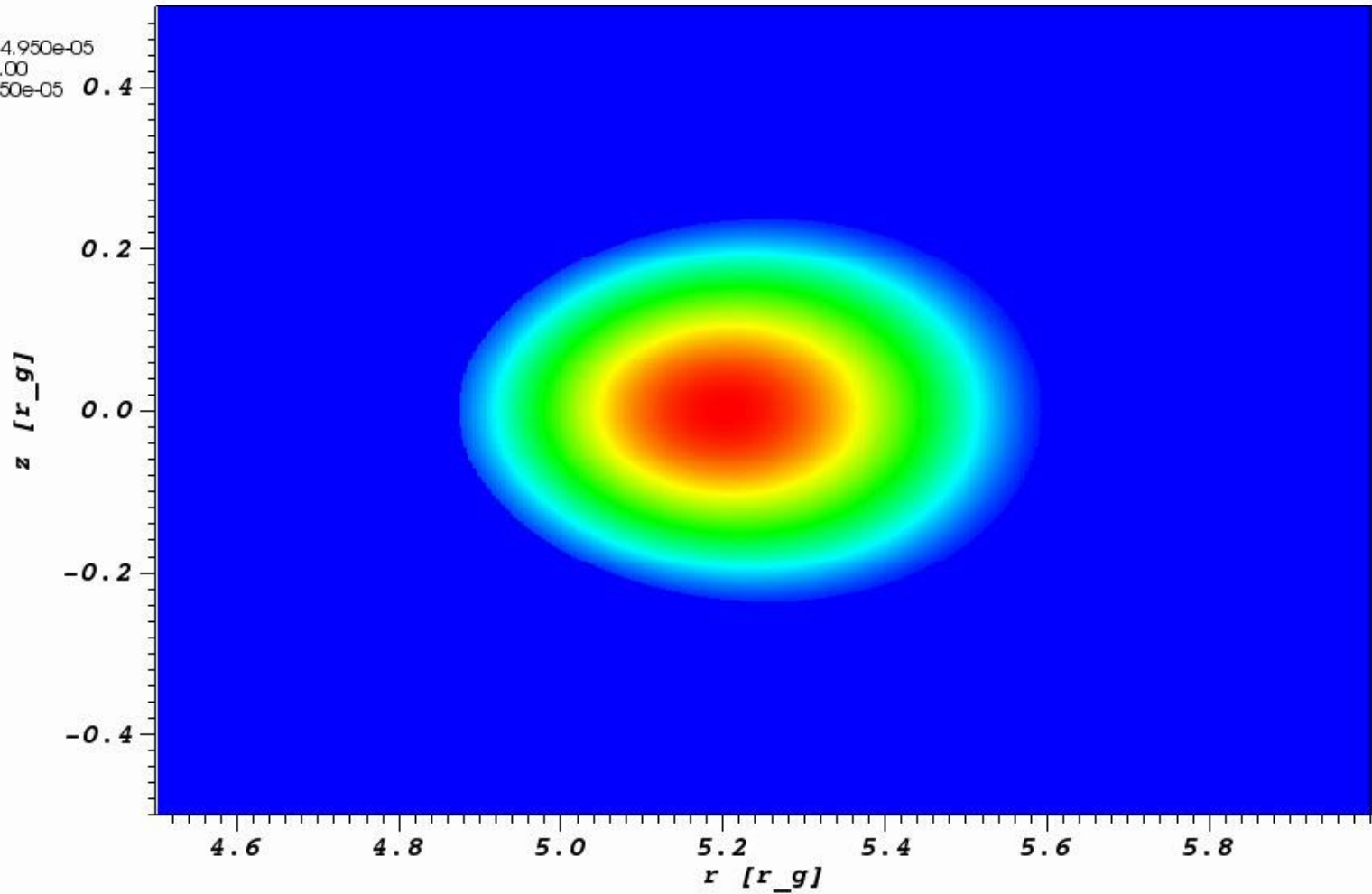
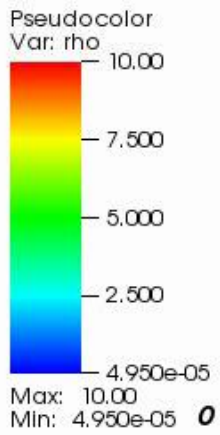


FIG. 5.—Poloidal velocity field for the radial epicyclic mode (*left*) and the vertical epicyclic mode (*right*) of a nonslender  $n = 3$  torus with  $\beta = 0.134589$  and pressure maximum at  $r = 7.293M$  (the same torus illustrated in Fig. 4, *right*).

Parthasarathy, Manousakis, WK, 2016 in press



DB: out-Master.cosmos++  
Cycle: 0      Time: 0

Mishra + 2016

Pseudocolor  
Var: massDensity

5.e-35

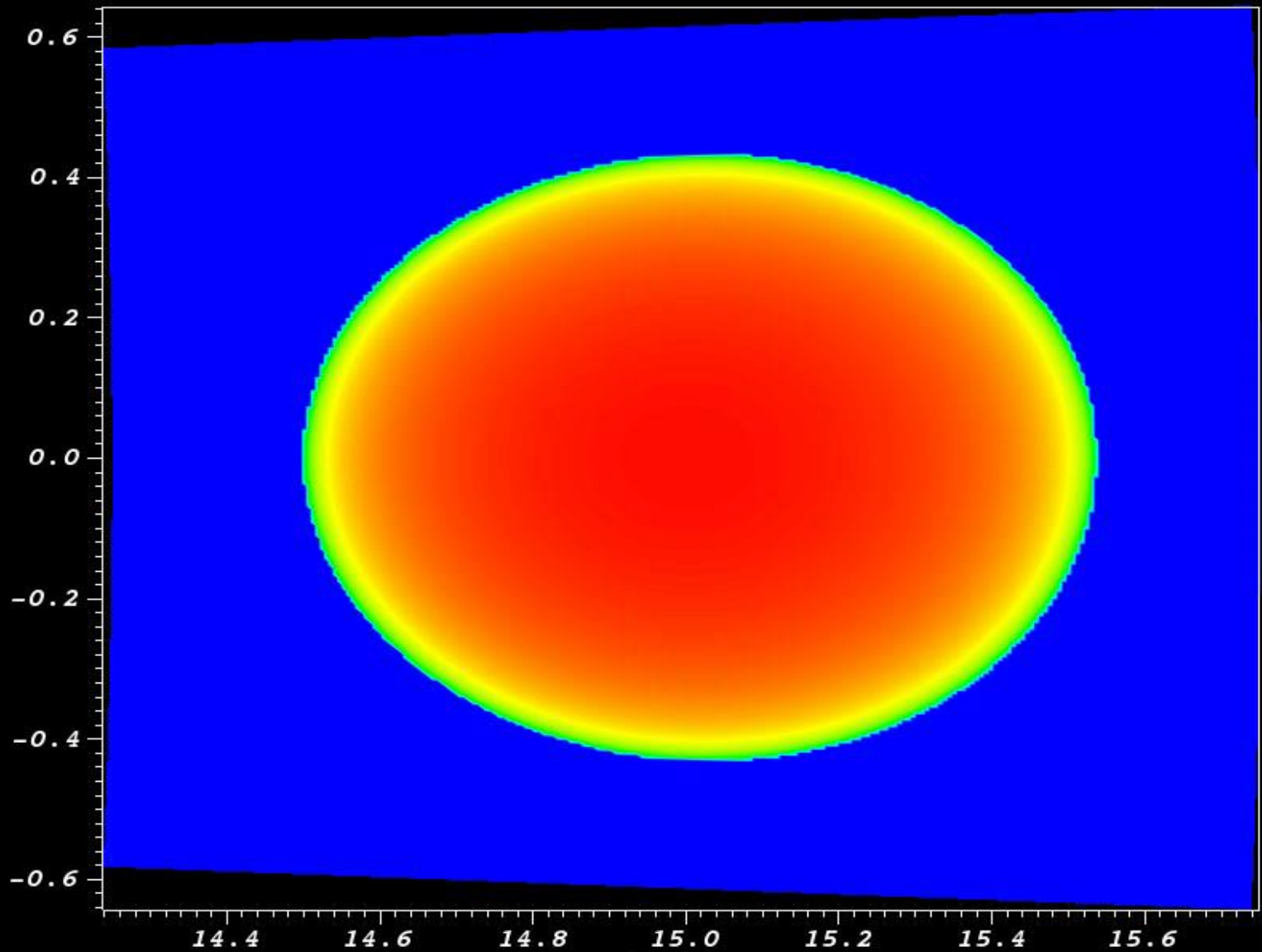
2.e-36

7.e-38

3.e-39

1.e-40

Y-AXIS





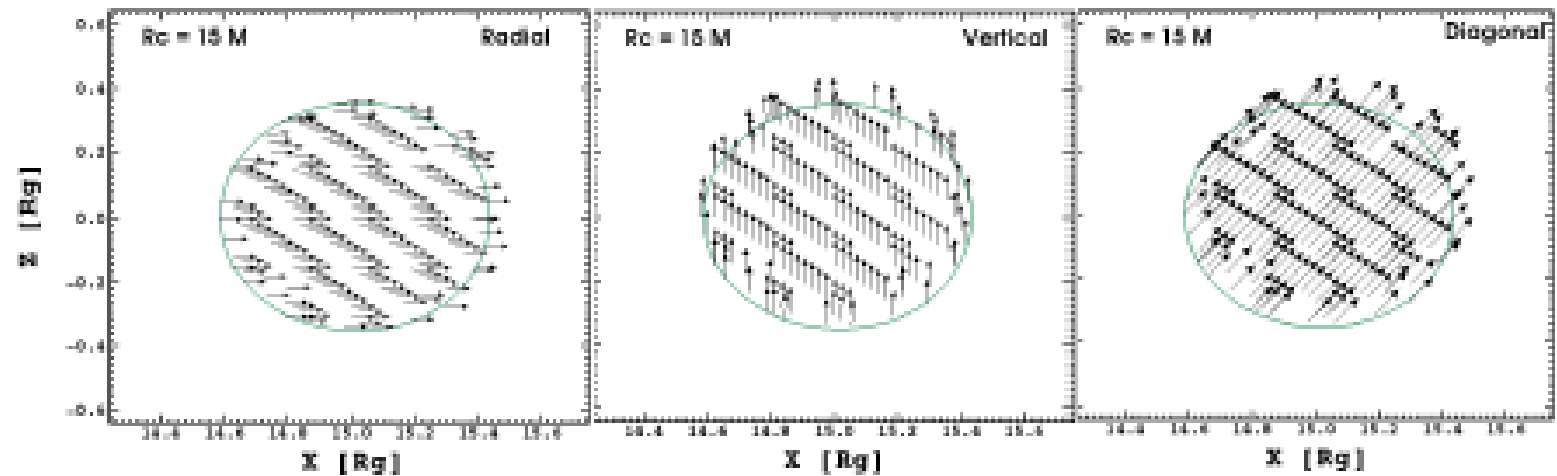
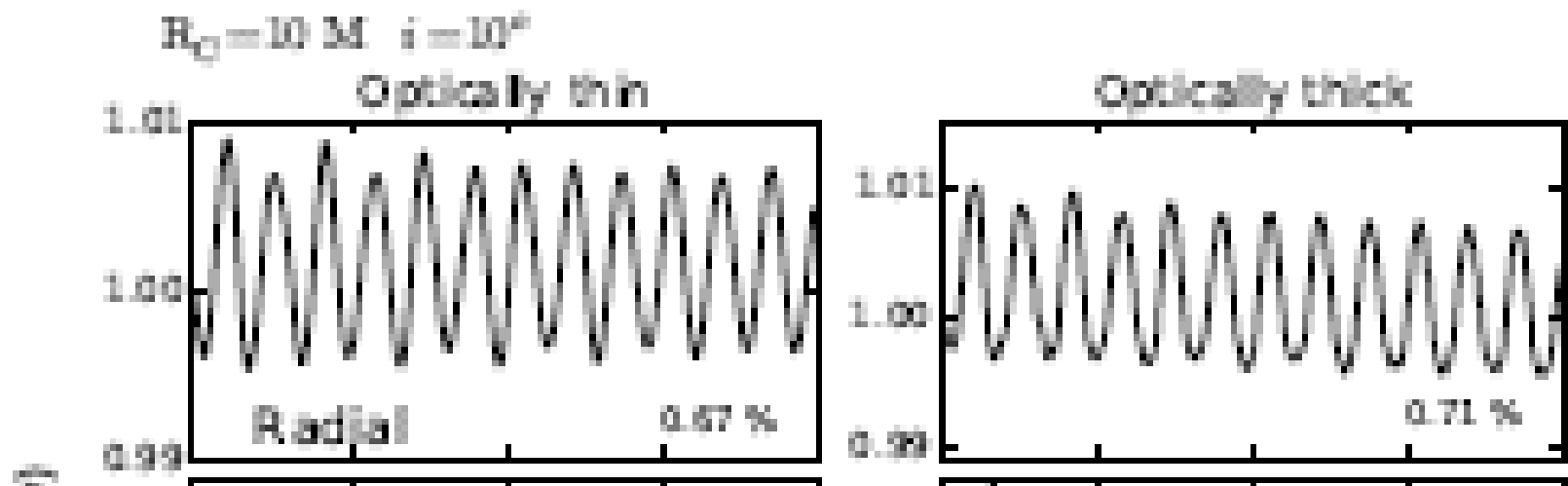
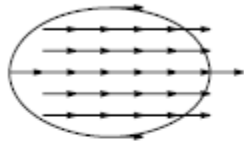


Figure 1. Three initial velocity perturbations to the torus. Plots only present the initial torus with pressure maximum at  $R_c = 15M$ . The torus setup at  $R_c = 10M$  looks qualitatively similar at the corresponding radial position.

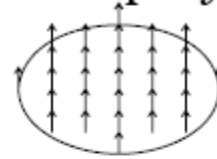


# Blaes et al 2006

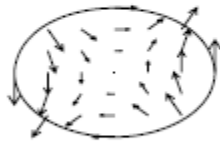
Radial Epicyclic (-+01)



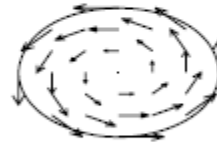
Vertical Epicyclic (+-01)



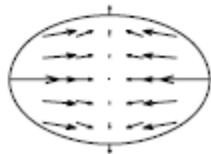
× Mode (- -02)



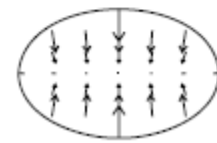
Inertial Mode (- -02)



+ Mode (+ +02)



Breathing Mode (+ +10)

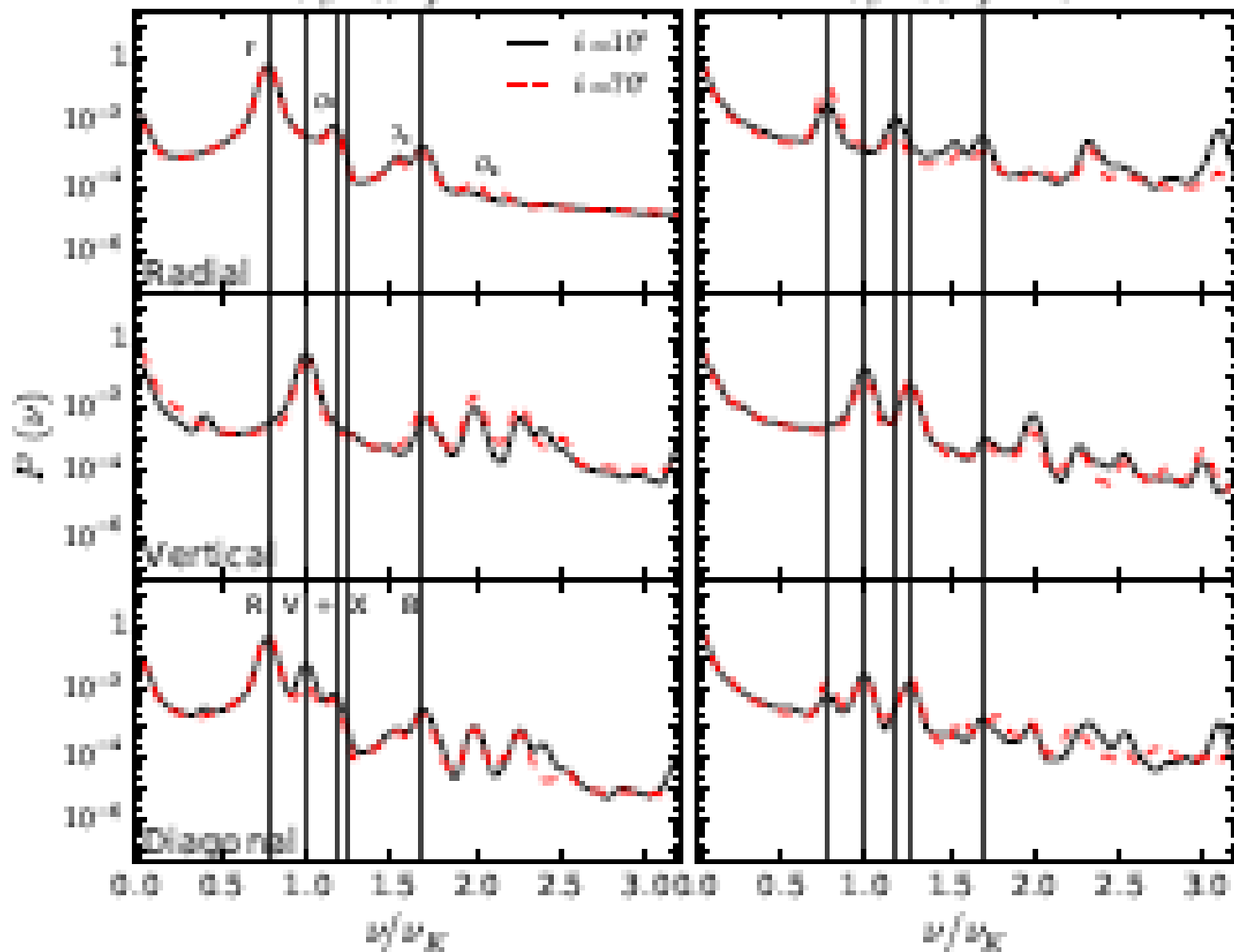


vertical lines: Radial, Vertical, +, X, Breathing

$R_s = 15 M$

Optically thin

Optically thick



PDS

17 minute QPO likely a counterpart of HF QPO in binary BH  
(450 Hz in GRO 1655-40)

HF QPOs present in PDS of ray-traced GR simulations of tori.  
The modes have been identified.

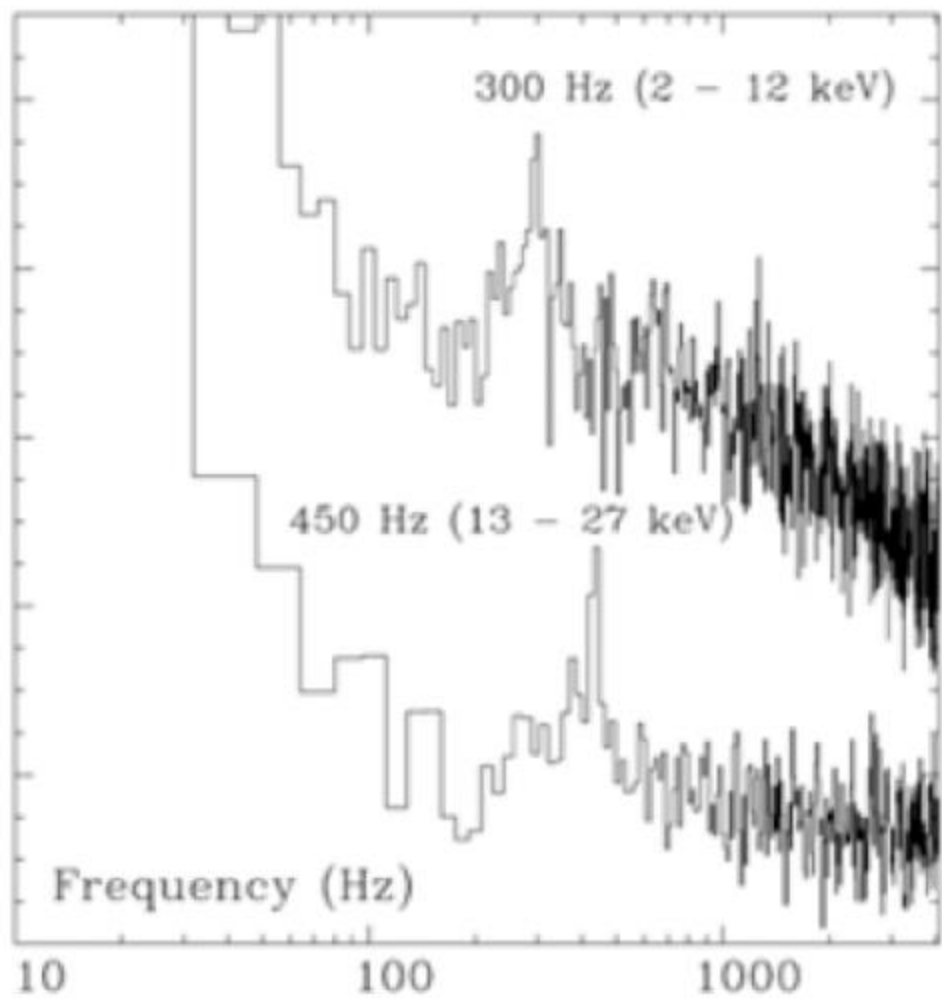
Which modes are present depends on the perturbation type.

Radial perturbations yield two modes (R, +) in  $\sim 3:2$  ratio

Ditto for vertical perturbations (V, B)

but only one pair ever seen in a given binary BH (to date?)





Abramowicz &  
 Kluźniak 2001,  
*A precise  
 measurement of BH  
 spin (A&A):*

'We note that the recently  
 discovered 450 Hz frequency in  
 the X-ray flux of the black hole  
 candidate GRO J1655-40 is in a  
**3:2 ratio** to the previously  
 known 300 Hz frequency...'

GRO J 1655-40 X-ray power spectra : discovery of  
 second HFQPO in a BH (Strohmayer 2001).