



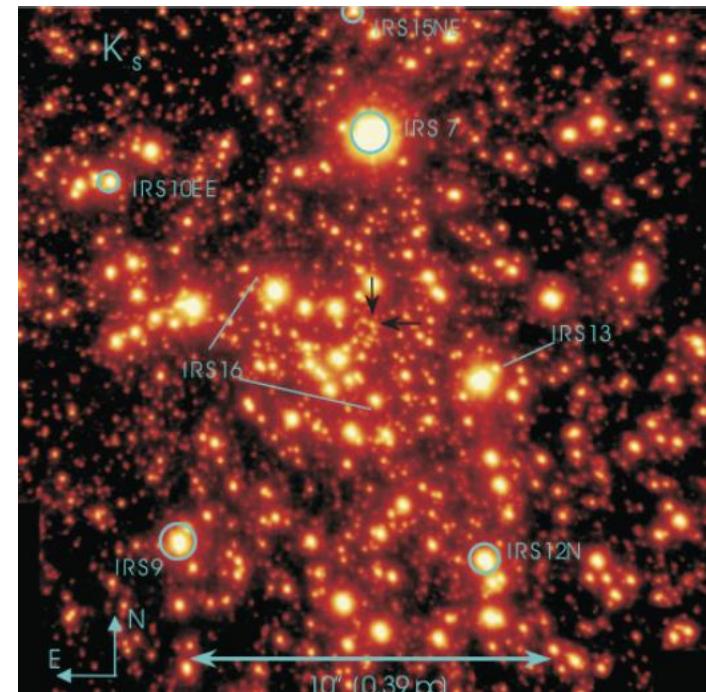
# Liquid crystals of stars and black holes at the centers of galaxies

**Bence Kocsis**

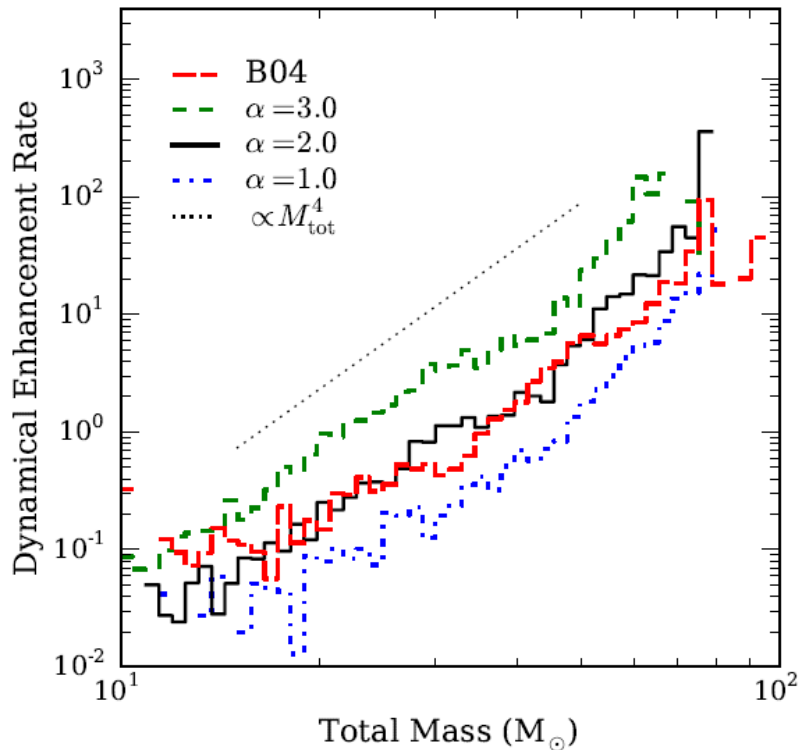
ERC Starting Grant group leader  
Eotvos University

In collaboration with  
Yohai Meiron, Zacharias Roupas,  
and Tim Brandt, Ryan O'Leary, Scott Tremaine

*Dynamics and accretion at the Galactic Center*  
February 9, 2016



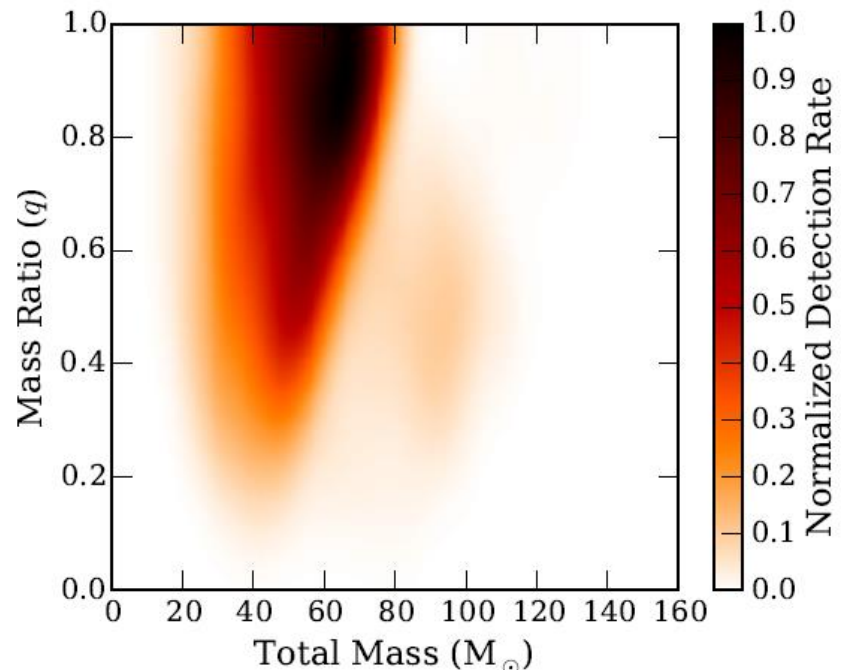
# Dynamical Formation Signatures of black hole binaries in future gravitational wave detections



Monte Carlo and Nbody simulations

*Advanced LIGO will measure GWs soon!*

- dynamical encounters lead to black hole mergers
- higher mass objects merge more often **by  $M^4$**
- GW detections can tell us about the BH IMF



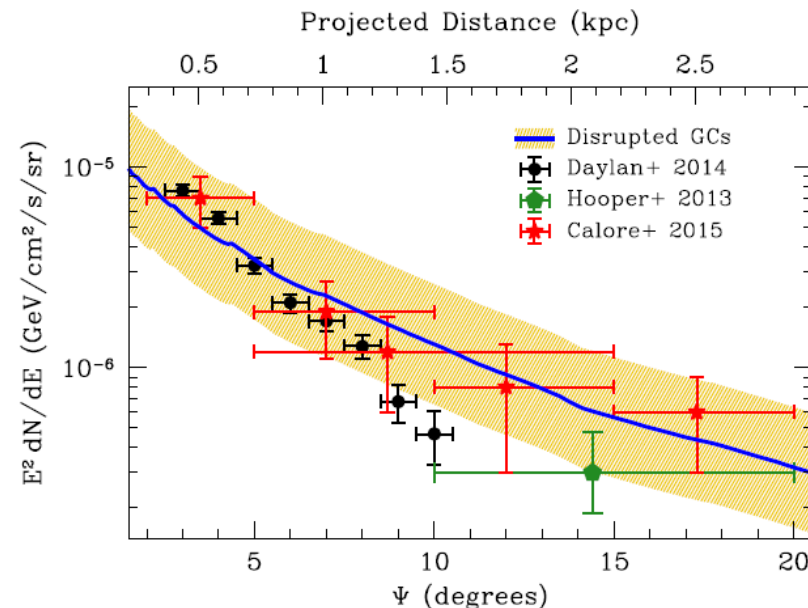
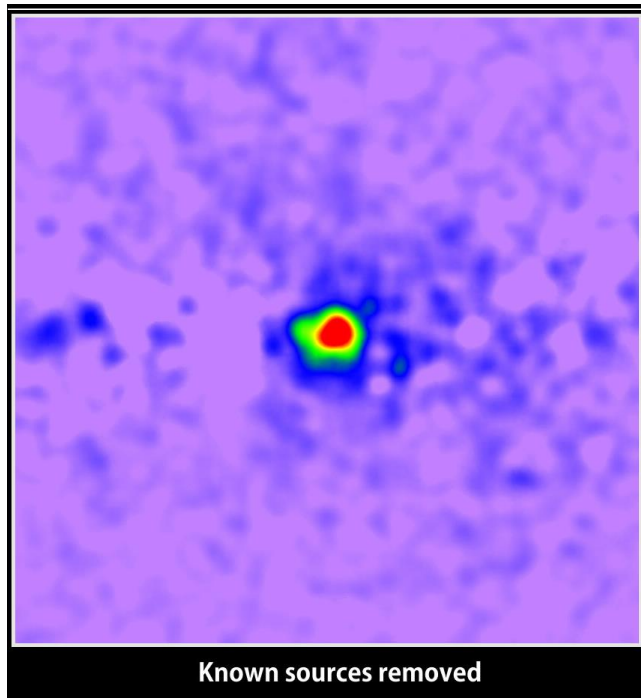
# Evidence for disrupted globular clusters?

A fraction of stars was delivered by infalling globular clusters

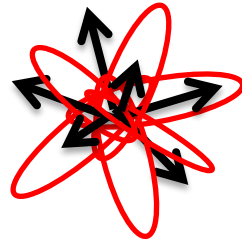
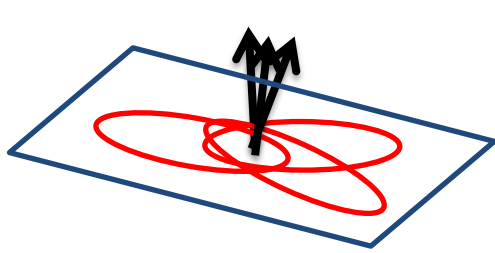
*Fermi measured excess gamma ray emission from the Galactic bulge*

- Millisecond pulsars match the observed spectrum
- Millisecond pulsars do not form in the bulge
- Infalling globular clusters delivered the needed population

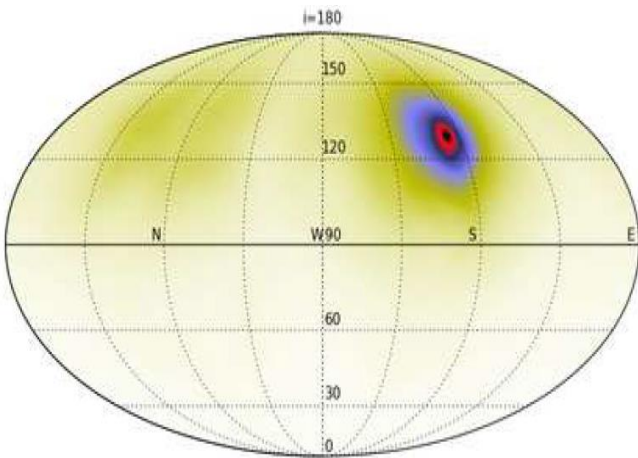
(No need to invoke dark matter annihilation to explain the gamma ray excess, just ordinary MSPs)



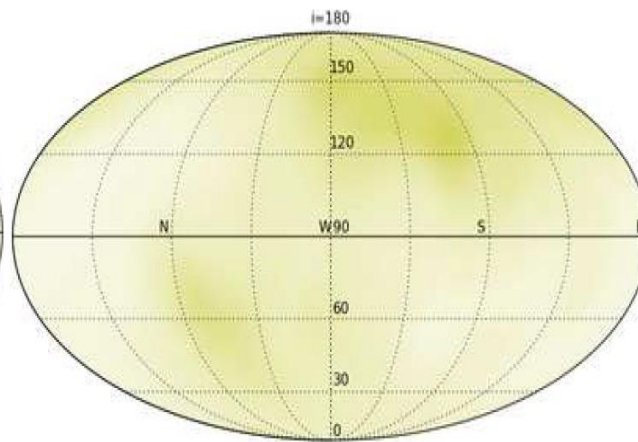
# Liquid crystals of stars to explain Anisotropy of massive stars



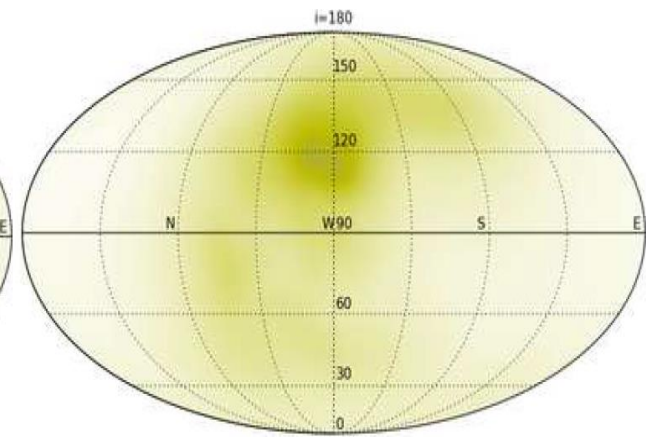
Yelda+ 2014



Inside 0.03-0.13 pc



Middle 0.13-0.27 pc

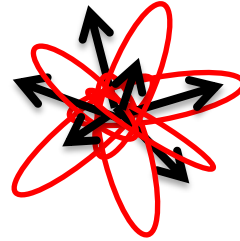
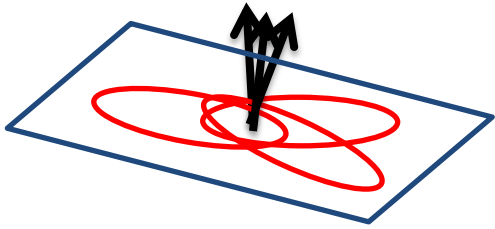


Outside 0.27-0.47 pc

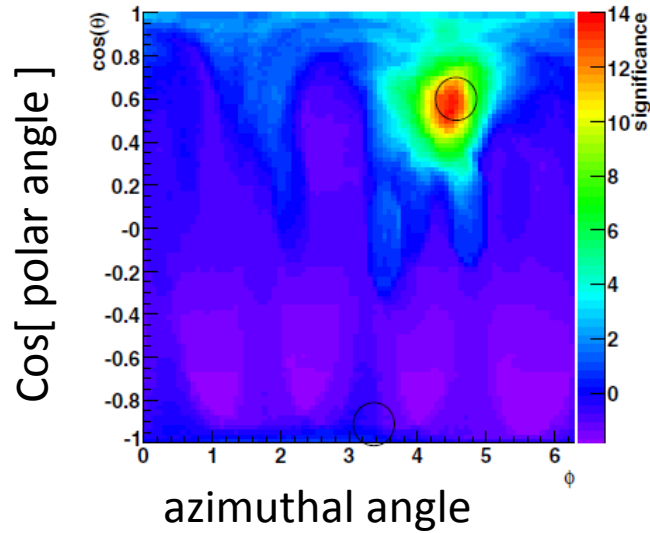
Density map of angular momentum vector **directions** for massive stars  
at three different locations



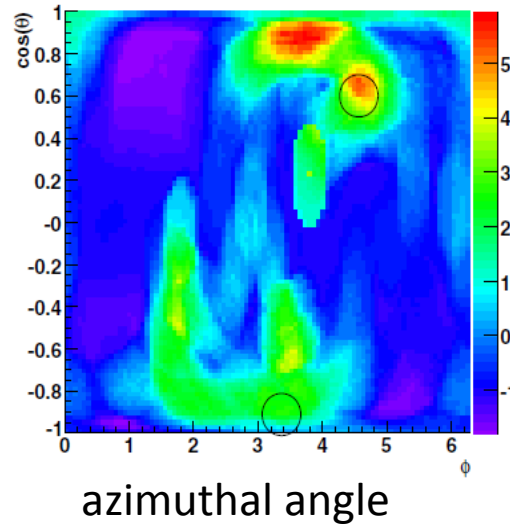
# Liquid crystals of stars to explain Anisotropy of massive stars



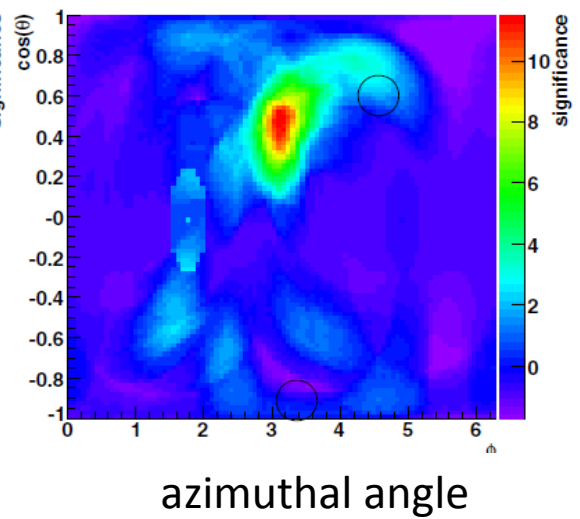
Bartko+ 2009



Inside 0.03-0.13 pc



Middle 0.13-0.27 pc



Outside 0.27-0.47 pc

Density map of angular momentum vector **directions** for massive stars  
at three different locations

# Liquid crystals of stars at the centers of galaxies

orbital period  $\ll$  in-plane precession  $\ll$  reorientation  $\ll$  semimajor axis change  
 [1–10<sup>4</sup> yr]                      [10<sup>4–5</sup> yr]                      [10<sup>5–7</sup> yr]                      [10<sup>9</sup> yr]

Persistent (“resonant”) torques **between smeared orbits** cause rapid reorientation  
 (Rauch & Tremaine 1996, Hopman & Alexander 2006, Eilon, Kuper, Alexander 2009, ...)

## Hamiltonian of resonant relaxation

Kocsis & Tremaine 2014

- Multipole expansion
- Leading order is the Hamiltonian of a liquid crystal

## Interesting analogy: Liquid crystals



(a) Normal liquid



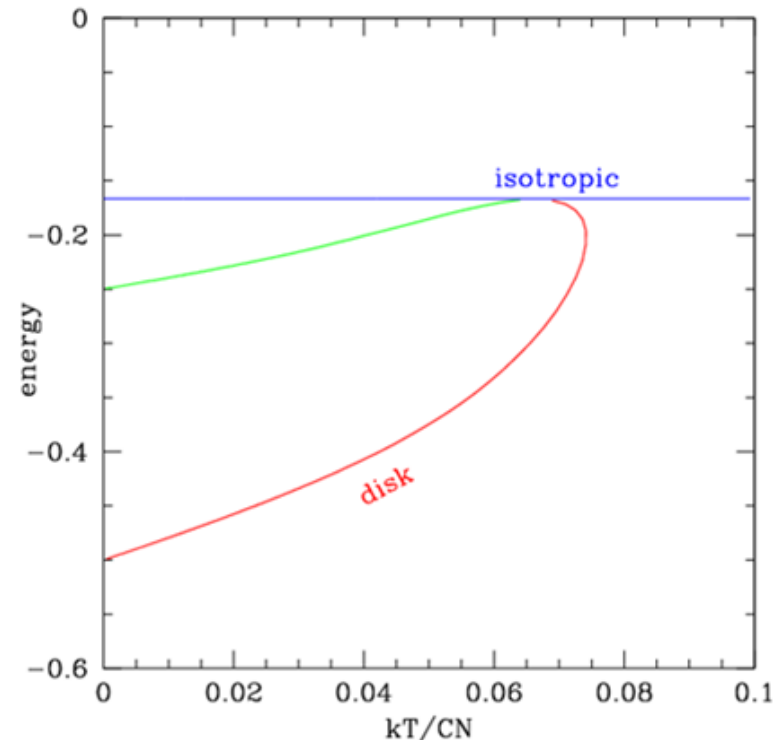
(b) Nematic liquid crystal



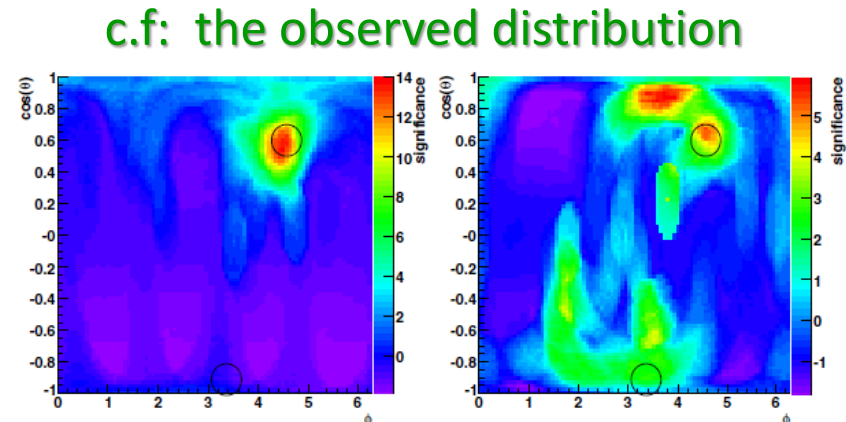
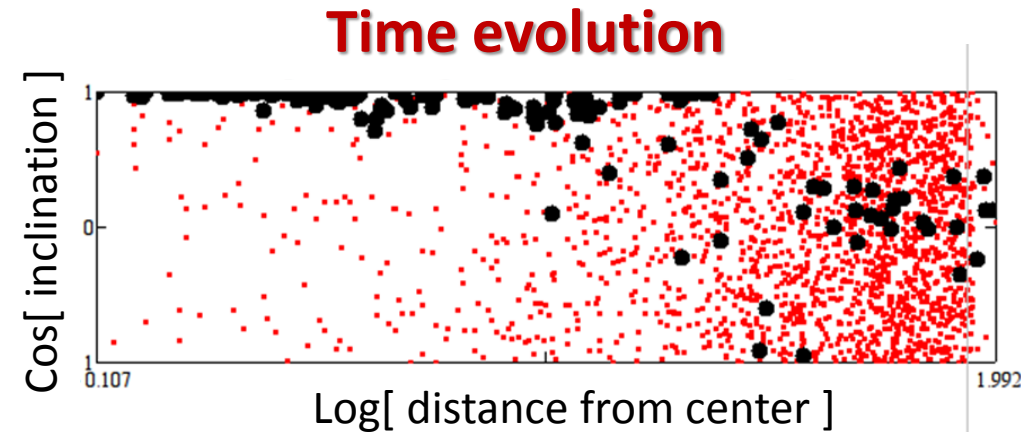
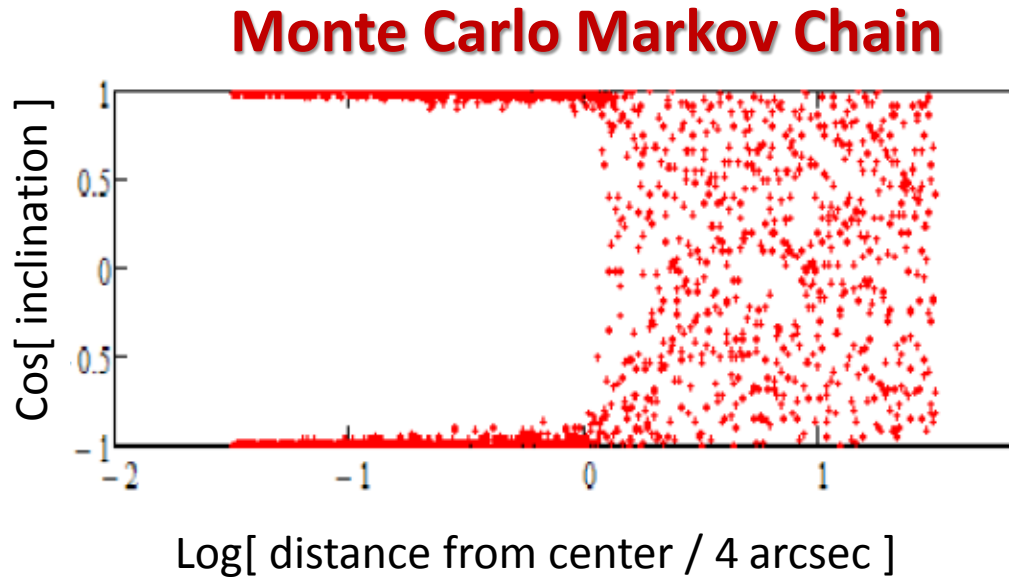
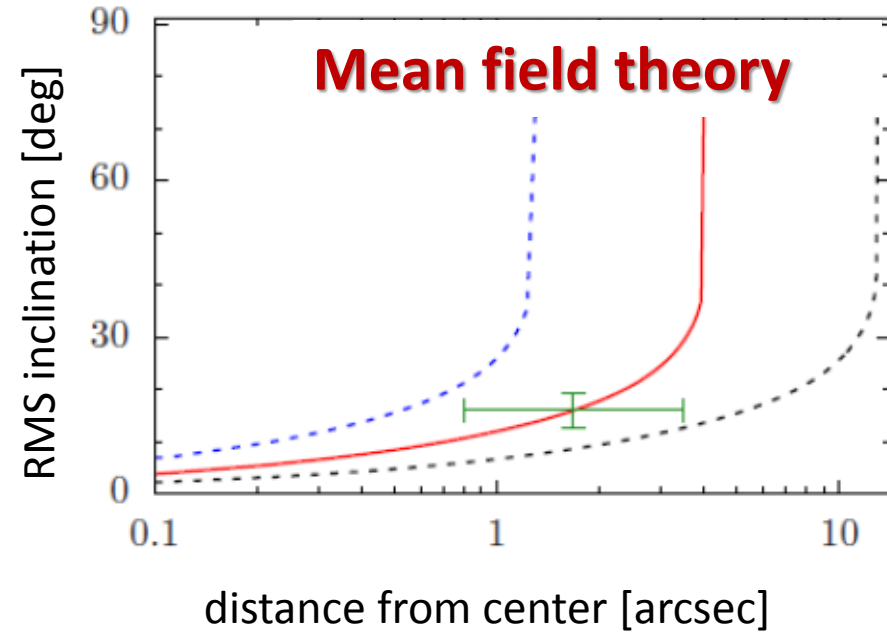
(c) Smectic A liquid crystal



(d) Smectic C liquid crystal



# Results

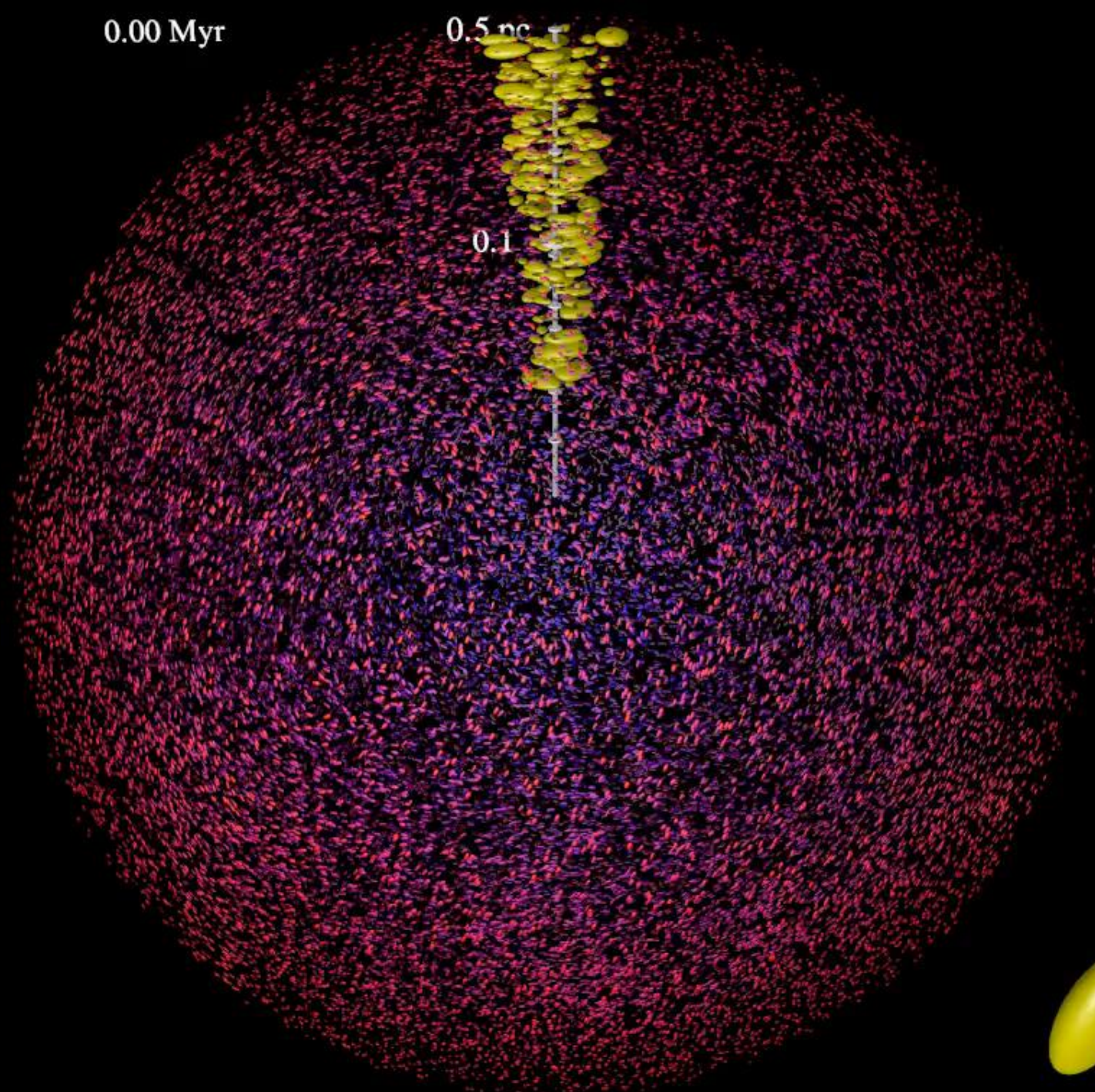




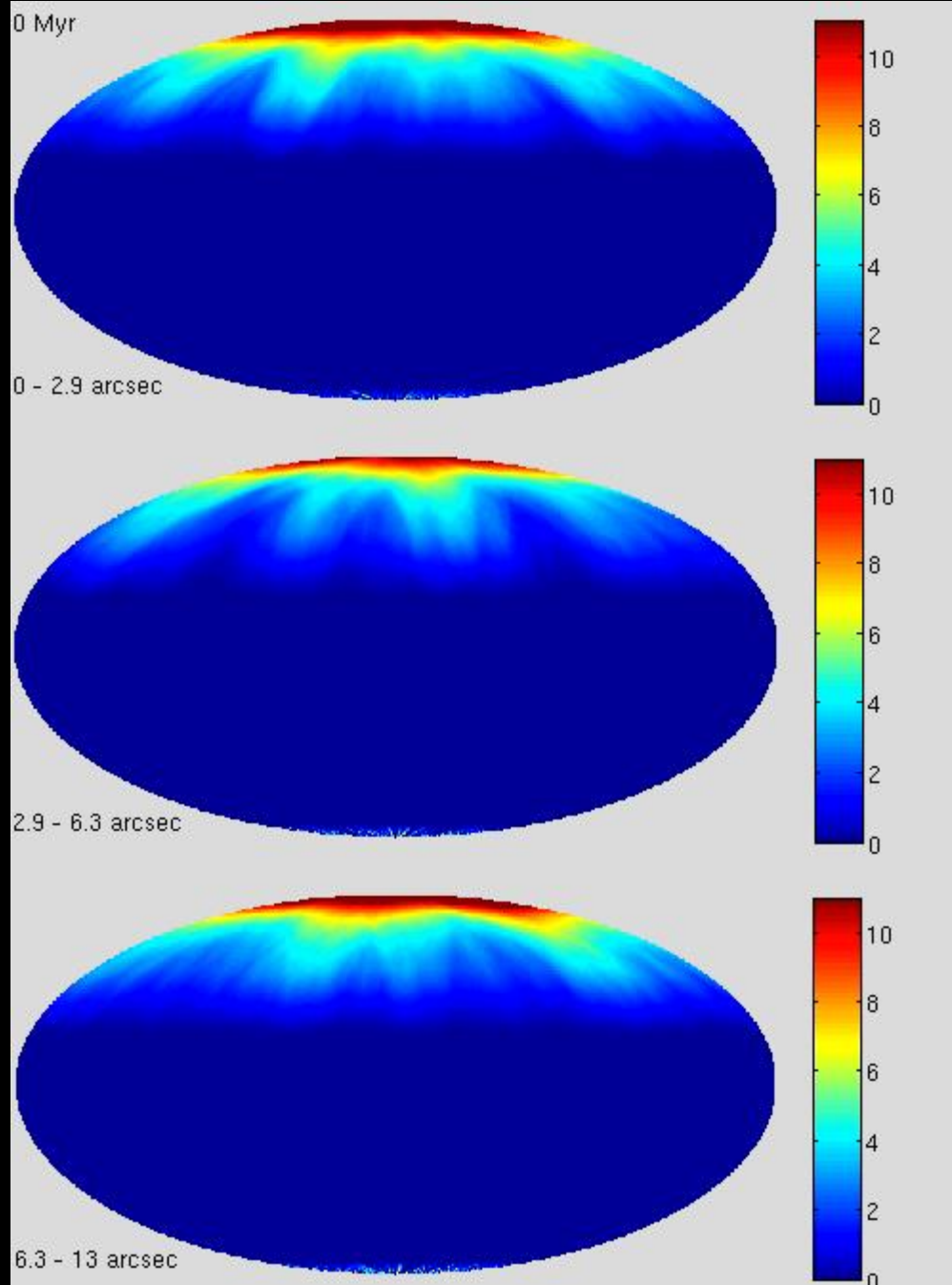
0.00 Myr

0.5 pc  $r$

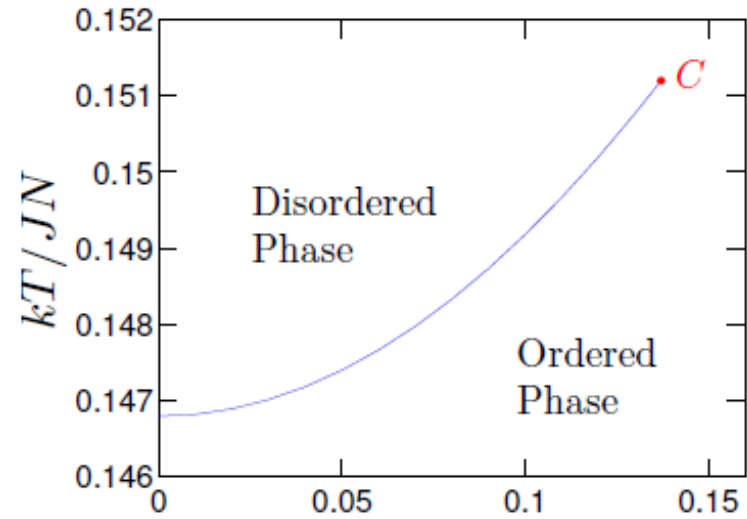
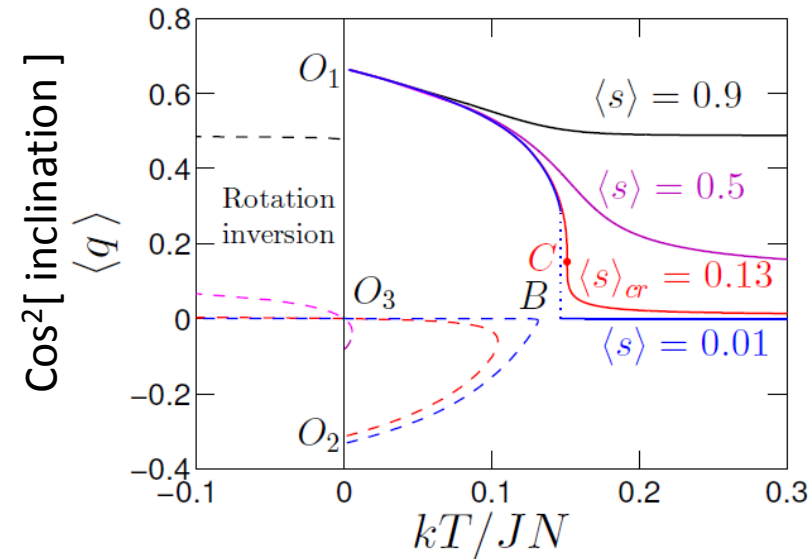
0.1



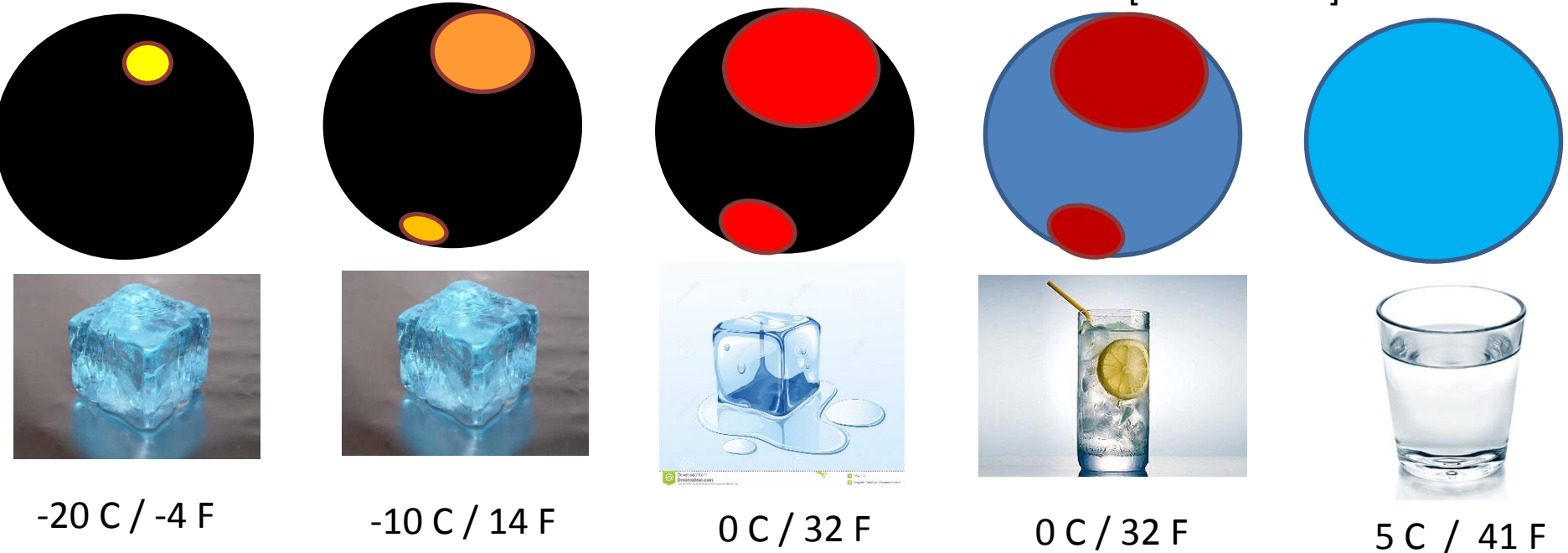




# Statistical equilibria



Distribution of angular momentum directions:

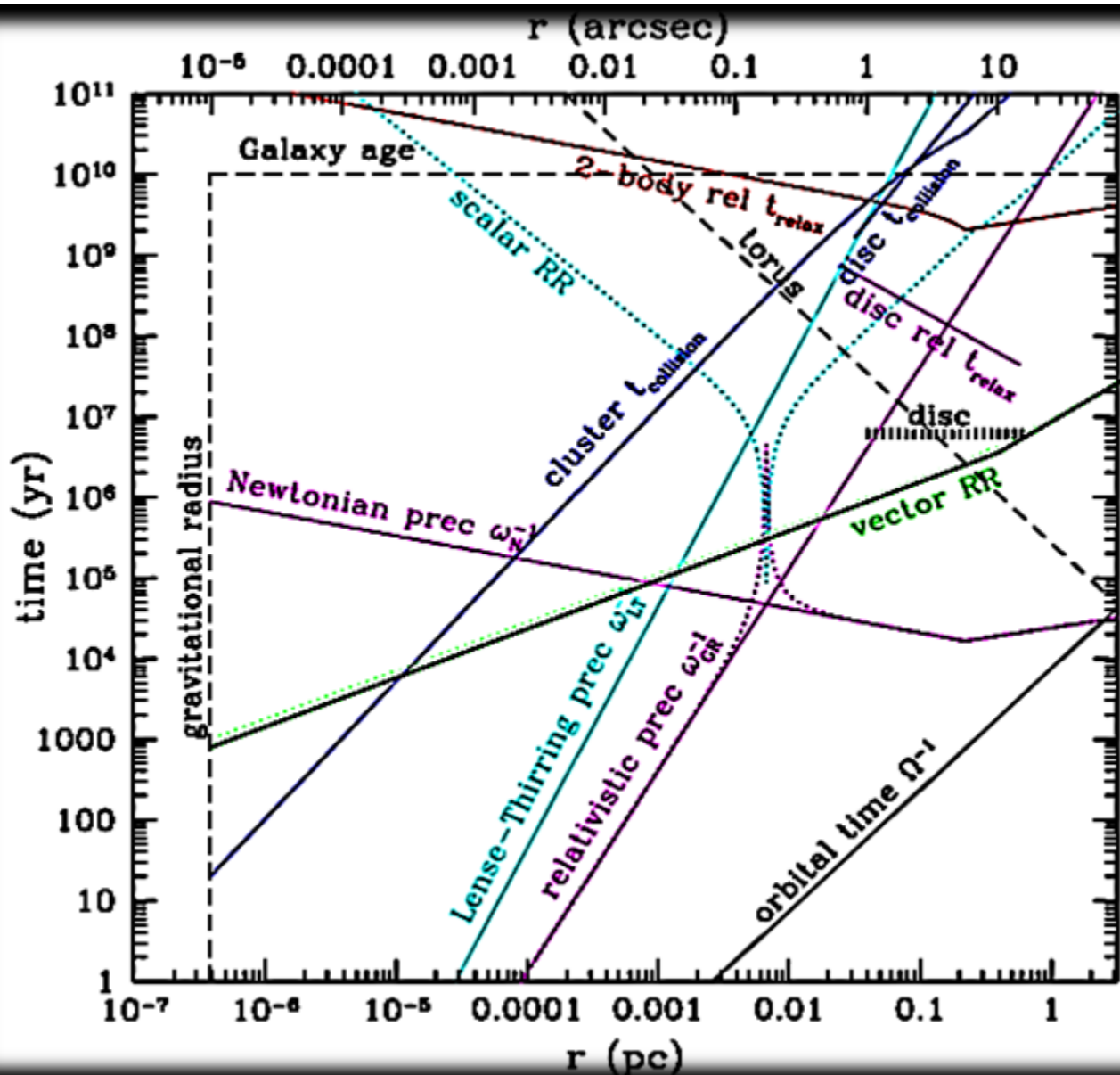


# Summary

- **LIGO** will constrain the **high-mass end** of the **BH mass function** in dense star clusters
- **Fermi** detected remains of **disrupted globular clusters**
- Orbital planes of stars **reorient resonantly** ( $\sim$ Myr)
  - **Liquid crystals** have a similar Hamiltonian
  - First order phase transition  $\rightarrow$  mixed phase (disk + spherical)
  - Young stars in the Galactic center show a similar structure
- Use this to
  - model the inclination distribution of different stellar types
  - predict the distribution of black holes



# Hierarchy of Interaction Timescales vs. radius



Semimajor axis change

Eccentricity change

Disk age

Re-orientation  
of orbital plane

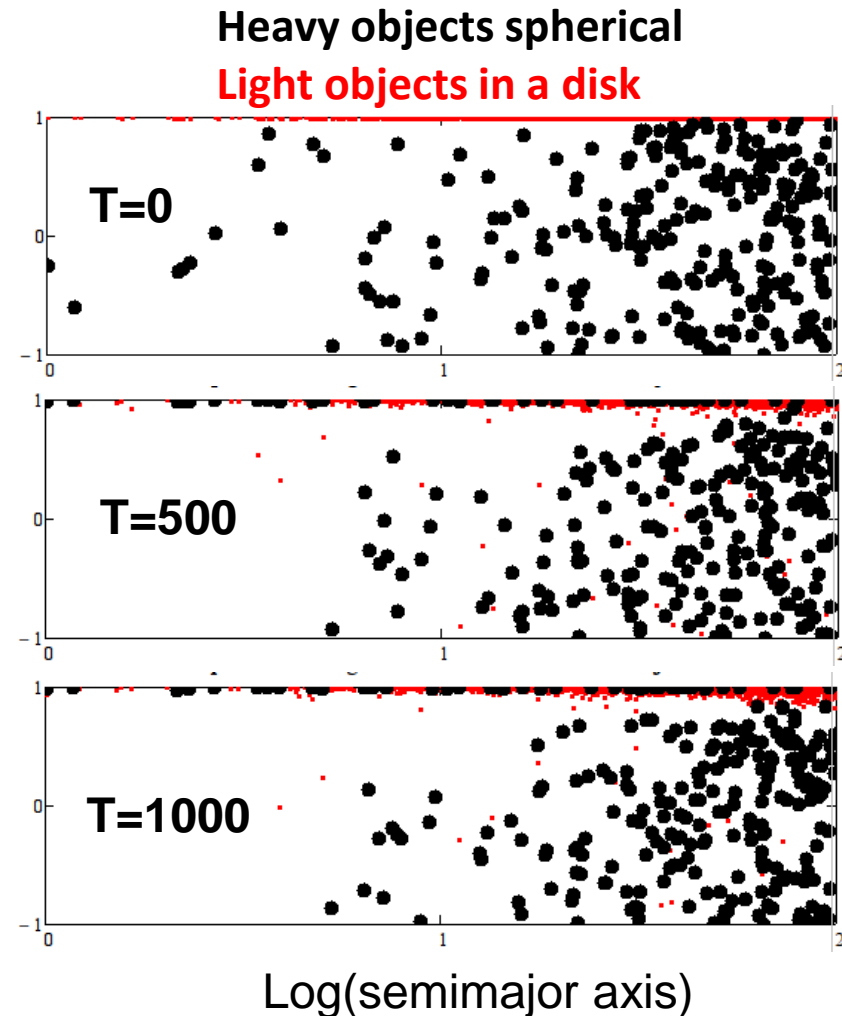
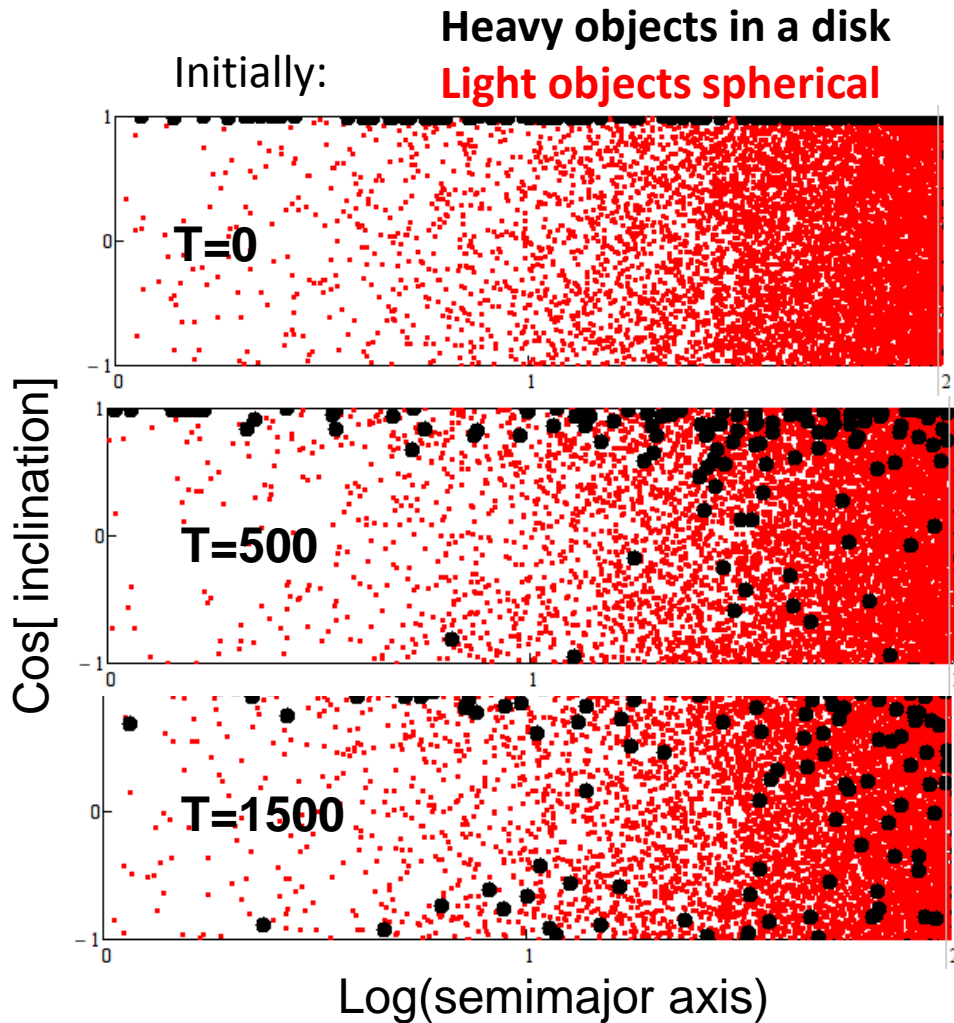
Precession in plane

Keplerian orbit  
around SMBH

Time scale

# Final state in the simulation

- Three snapshots in two simulations



# Statistical equilibrium

- Objects fill up phase space uniformly

Find maximum entropy configuration under constraints  $E_{\text{tot}} = \text{const}$

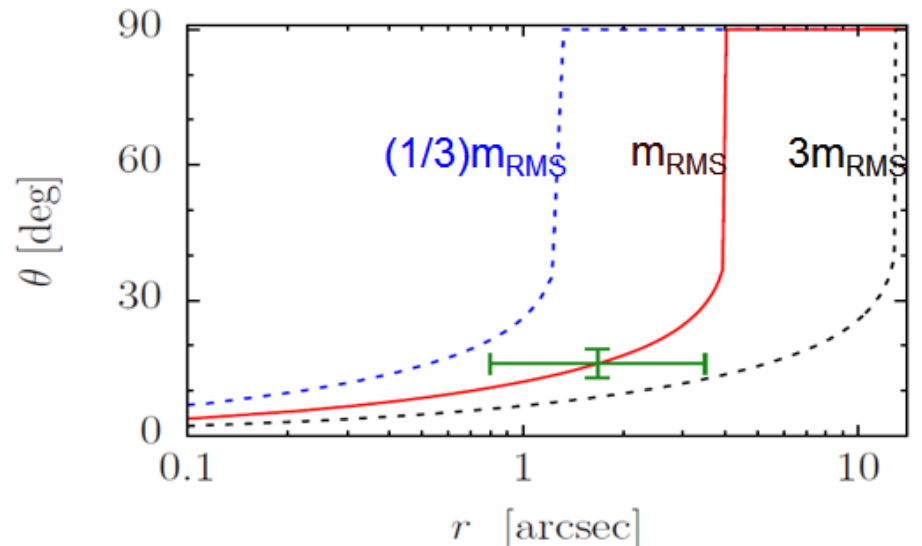
$$\mathbf{L}_{\text{tot}} = \text{const}$$

$$f(\mathbf{L}) = C \exp\left(-\frac{E(\mathbf{L})}{kT}\right)$$

Phase transition  
in inclination

- Mean field theory

- Maier & Saupe (1959)
- keep only the quadrupole term
- assume interaction dominated by stars on same radius
- self-consistency equation for quadrupole moment

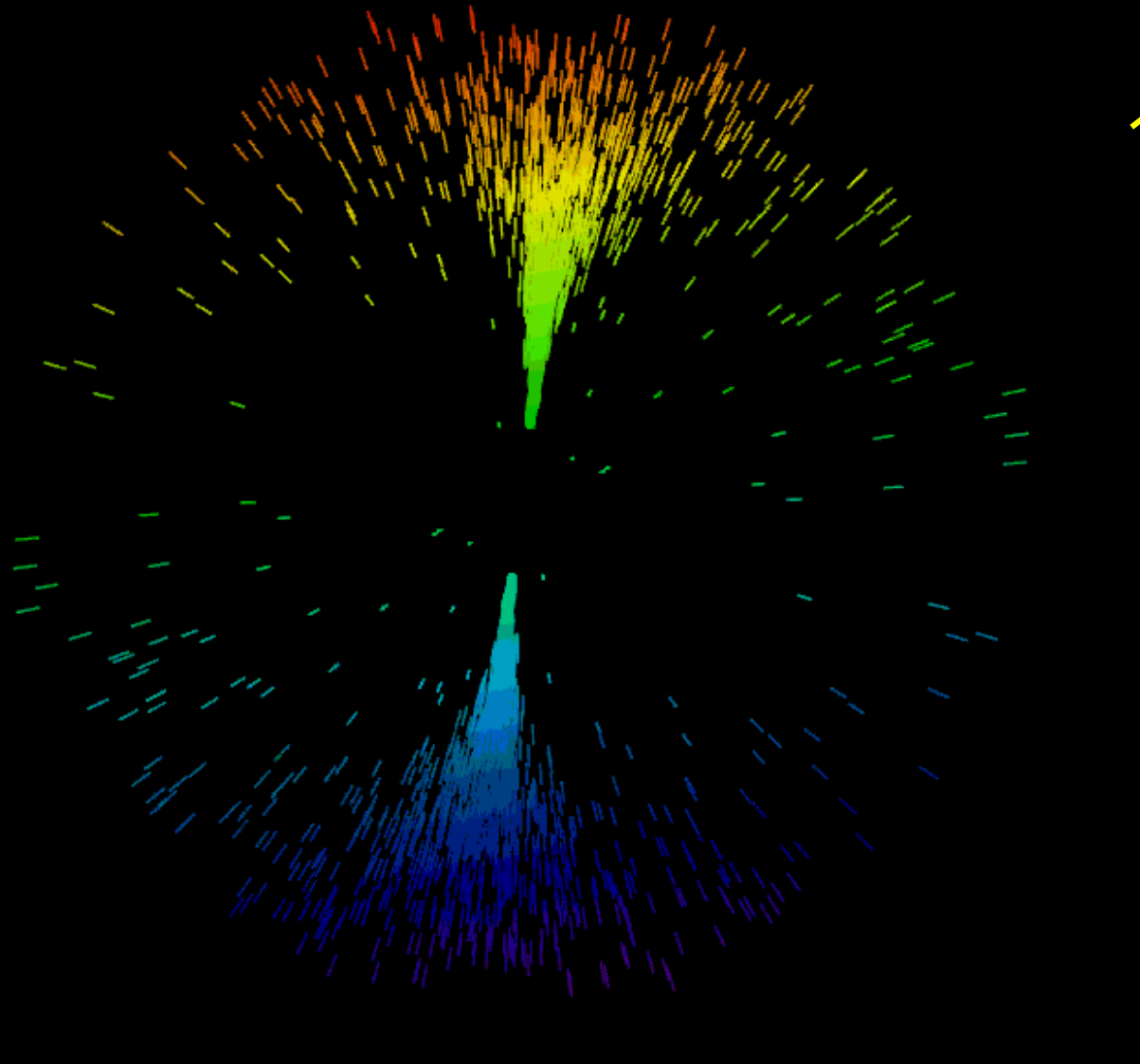




# Thermal equilibrium (maximum entropy)

orbit normals as a function of radius

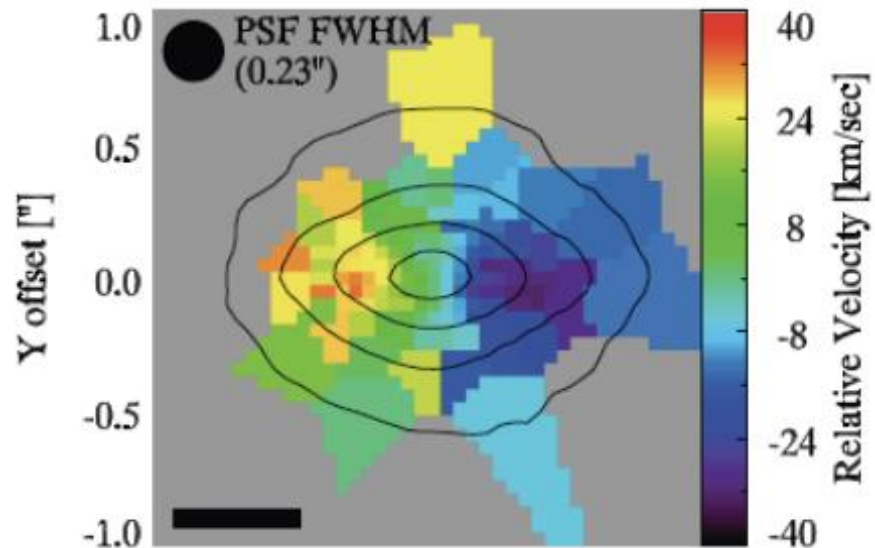
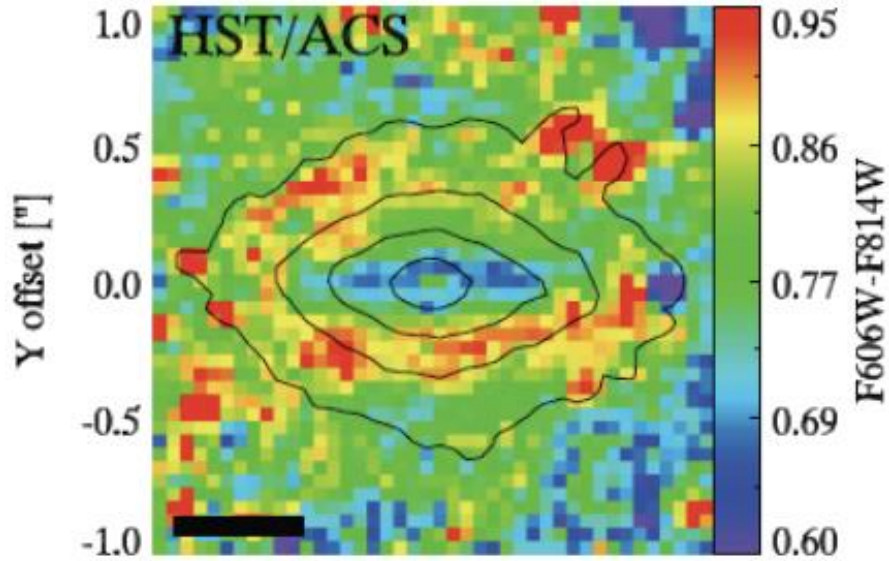
outer  
radius  
inner  
radius



- initially warped disk
- Stars:
  - same mass, eccentricity
- conserve total energy  
“microcanonical ensemble”

**Phase transition  
in inclination**

# Nuclear Star Clusters



## The densest stellar environments

Multiple stellar populations

Walcher+ '06, Rossa+ '06, Seth+ 06, 08, 10

- old, red spheroid
- young, blue disk
- Both rotate
- In many edge-on galaxies:  
counterrotating with respect to galaxy