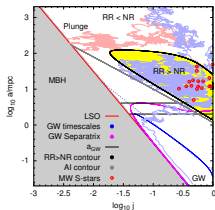


Relativistic loss-cone dynamics: Implications for the Galactic Center

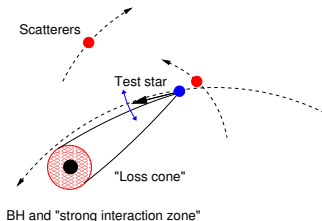
Tal Alexander

Weizmann Institute of Science



The stellar dynamical loss-cone problem:

How do stars in a galactic nucleus interact *strongly* with a massive black hole (MBH) and/or fall into it, and at what rates?



Implications

Plunge processes:

Tidal disruption flares^{1,2}, tidal detonation³, tidal scattering⁴, gravitational wave (GW) flares

Inspiral processes:

GW extreme mass ratio inspirals (EMRIs)^{1,2,5}, tidal squeezars⁶, accretion disk capture

Exotic stellar populations near MBHs^{7,8,9}

MBH+stars formation and evolution^{10,11,12,13}

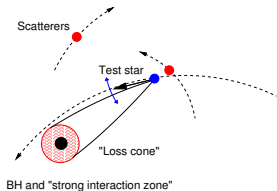
How do galactic nuclei randomize and relax?

- └ Getting stars to the MBH
- └ Randomization by relaxation

Relaxation near a MBH

Non-coherent relaxation (NR: E, J)

Point—point interactions



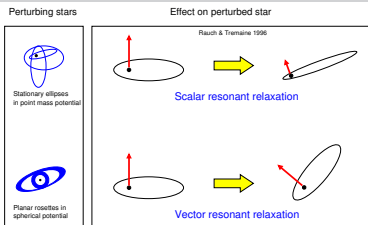
$$Q = M_{\bullet} / M_{\star}$$

$$T_{NR} \sim [Q^2 P / N_{\star}] / \log Q$$

$1 / \log Q$: relaxation boost from close encounters

Resonant relaxation (RR: J)

Orbit-orbit interactions



$$T_{RR} \sim [Q^2 P / N_{\star}] P / t_{\text{coh}}$$

P / t_{coh} : relaxation boost from long coherence

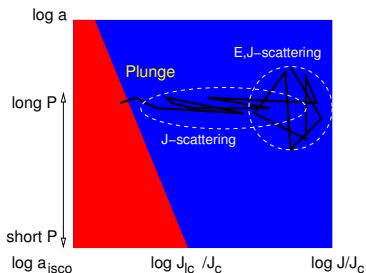
Near MBH: $T_{RR} / T_{NR} \sim \log Q (P / t_{\text{coh}}) \ll 1$

Fast evolution to $J \rightarrow 0$: Strong interaction with the MBH

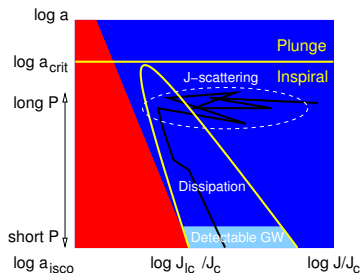
- └ Getting stars to the MBH
- └ Randomization by relaxation

The “classical” (pre-RR) loss-cone: Plunge vs inspiral

Loss primarily by J -relaxation:  $T_J \sim j^2 T_E$ $j = J/J_c(E)$



(Lightman & Shapiro 1977; Cohn & Kulsrud 1978)



(TA & Hopman 2003; Hopman & TA 2005)

$$\Gamma_{plunge} \sim N_*(< r_h) / \langle \log(J_c/J_{lc}) T_E \rangle$$

$$\Gamma_{inspiral} \sim N_* [< r_{crit}(T_E)] / \langle \log(J_c/J_{lc}) T_E \rangle$$

$$\Gamma_{inspiral} \sim O(0.01) \Gamma_{plunge}$$

↳ Getting stars to the MBH

↳ Randomization by relaxation

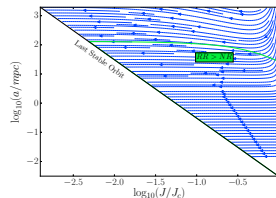
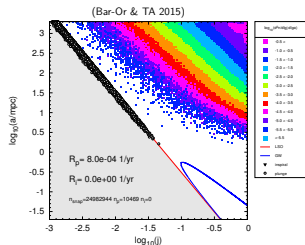
The “danger” of unquenched RR: No inner cusp

(No GR stars, no GW EMRIs, no ...)

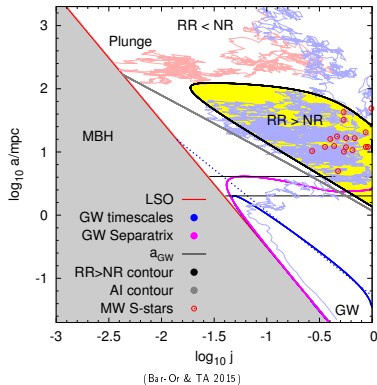
The “fortunate coincidence” conjecture:

(Hopman & TA 2006)

- ▶ Unquenched, RR drives all stars to plunge orbits (no EMRIs!).
- ▶ $\mathcal{O}(\beta^2 j^{-2})$ GR in-plane Schwarzschild precession becomes significant before $\mathcal{O}(\beta^5/2 j^{-7} Q^{-1})$ GW dissipation.
- ▶ GR precession quenches RR and allows EMRIs to proceed unperturbed, decoupled from the background stars.



The relativistic loss-cone



The η -formalism

Stellar dynamics in the presence of correlated noise

(Ben Bar-Or's talk)

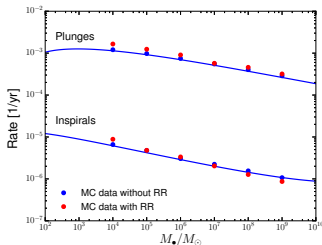
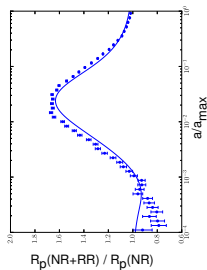
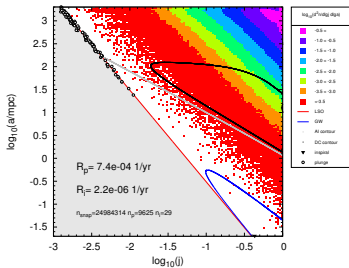
- Adiabatic invariance^(*) quenches RR at low- j
- NR dominates evolution on long time scales
- Dynamical modeling of the relativistic loss-cone

Effective RR diffusion that express correlated noise and secular precessions, together with NR diffusion and GW dissipation, provide a powerful scalable Monte Carlo tool for modeling long-term dynamics and loss-rates of galactic nuclei in the realistic $N_* \gg 1$ limit^(†).

* Correct form and interpretation of the 'Schwarzschild Barrier' (Merriù, TA, Mikula & Will 2013).

† Validated against N -body results in the low- N_* regime.

GW EMRI and tidal disruption rates in steady state



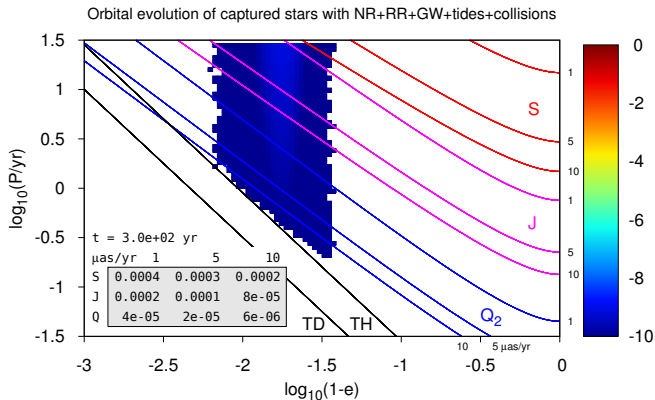
Galactic nucleus model ("MWEG")

- GR+mass precession
- GW+NR+RR
- Smooth noise+mass quenching
- Adiabatic invariance saves EMRIs:
- "Fortunate coincidence" validated.

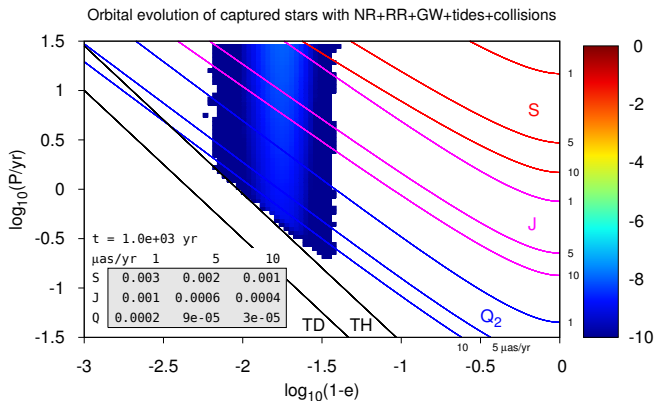
The hunt for relativistic stars for testing strong gravity^{1,2,3}

- ▶ **Option 1: No old cusp in inner Galactic center** (inner RG cusp missing^{4,5,6})
 - ▶ All young stars inside $\lesssim 0.01$ pc observed—none strongly relativistic.
 - ▶ Low stellar density \Rightarrow very slow dynamical evolution.
 - ▶ \Rightarrow No *local* stellar targets for tests of strong GR.
- ▶ **Option 2: Dark cusp of stellar remnants + old stars further out**
 - ▶ Rapid *e*-evolution (RR), but slower *a*-evolution (NR).
 - ▶ Stellar destruction ($\overline{T}_* \sim 5 \times 10^7$ yr) faster than T_E at $\mathcal{O}(1$ pc).
 - ▶ Strong depletion of *local* strongly relativistic stars.
- ▶ **Option 3: Dark cusp of stellar remnants + tidally-captured stars**
 - ▶ Low-mass equivalents of S-stars / Hyper-velocity B-stars.
 - ▶ Fast, continuous supply rate if scaled by S-stars.

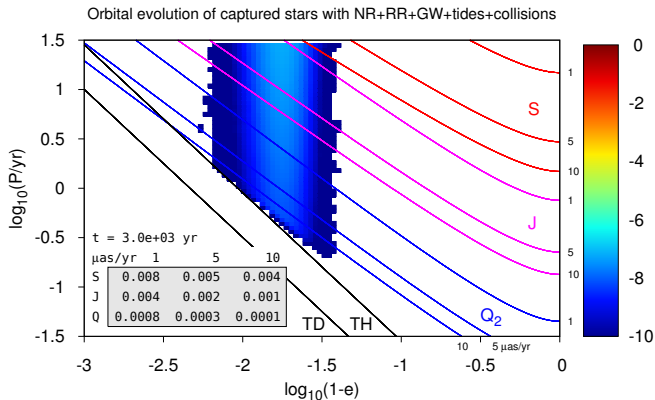
Evolution of tidally-captured relativistic stars in a dark cusp



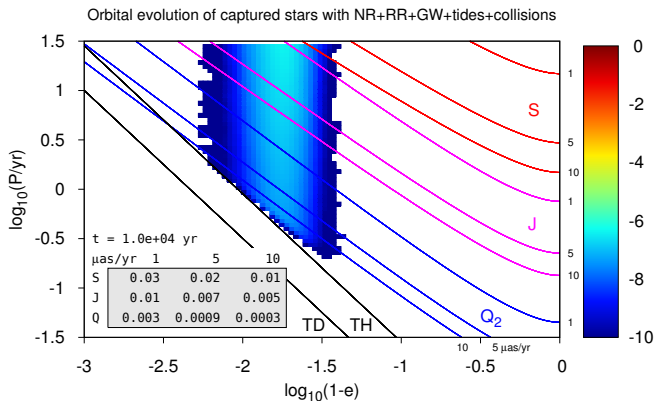
Evolution of tidally-captured relativistic stars in a dark cusp



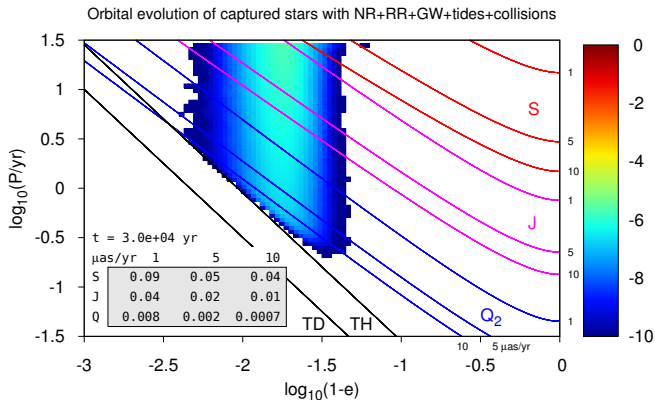
Evolution of tidally-captured relativistic stars in a dark cusp



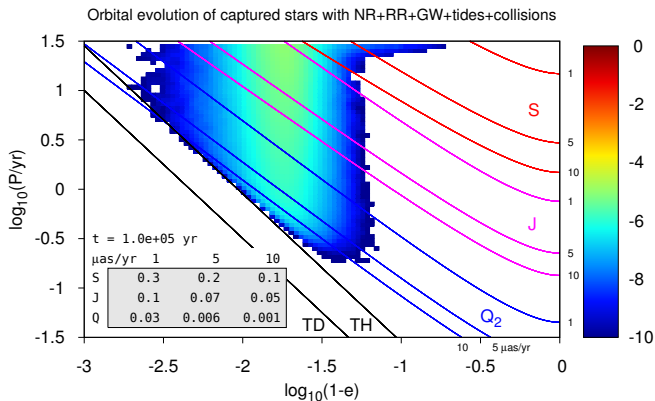
Evolution of tidally-captured relativistic stars in a dark cusp



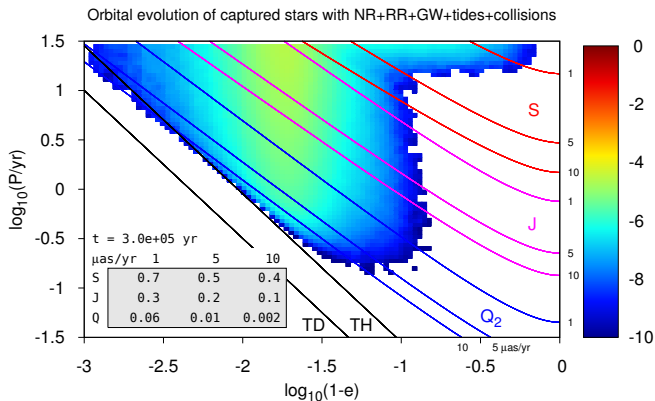
Evolution of tidally-captured relativistic stars in a dark cusp



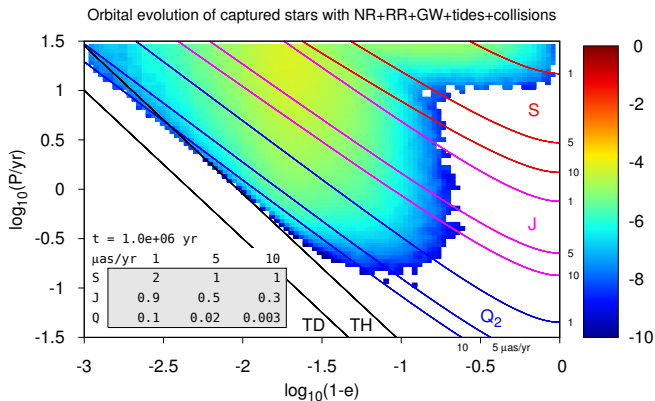
Evolution of tidally-captured relativistic stars in a dark cusp



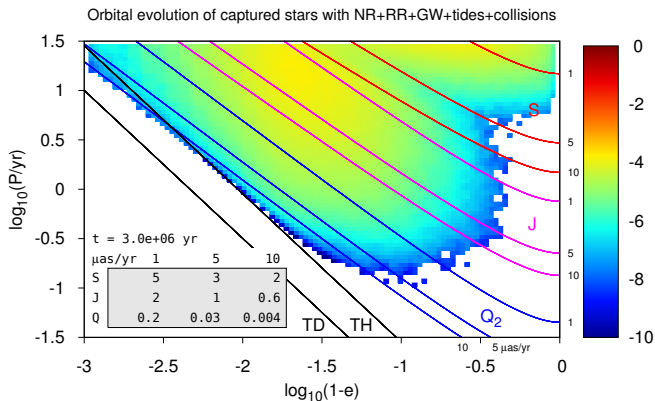
Evolution of tidally-captured relativistic stars in a dark cusp



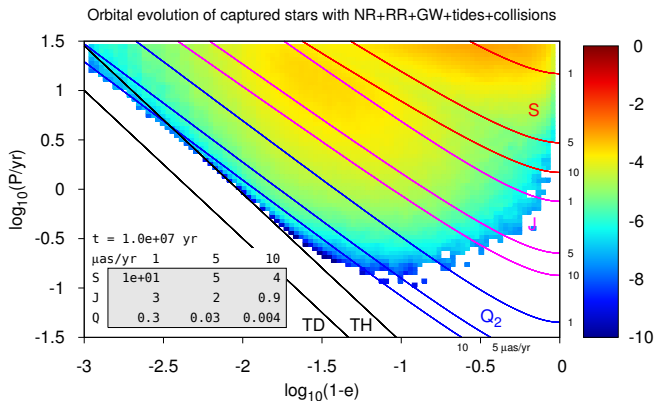
Evolution of tidally-captured relativistic stars in a dark cusp



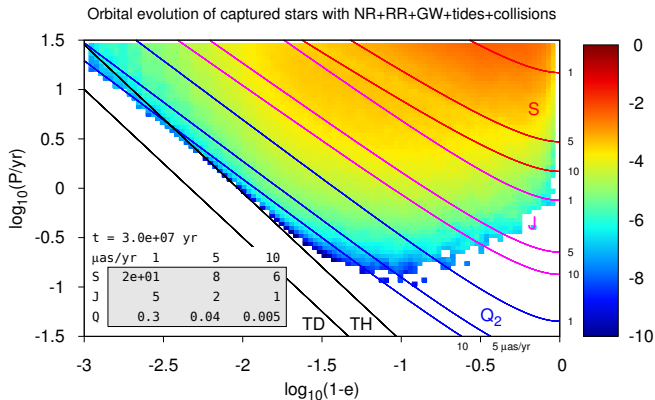
Evolution of tidally-captured relativistic stars in a dark cusp



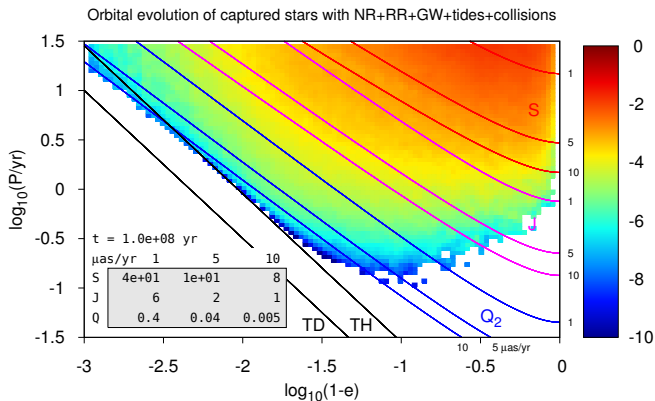
Evolution of tidally-captured relativistic stars in a dark cusp



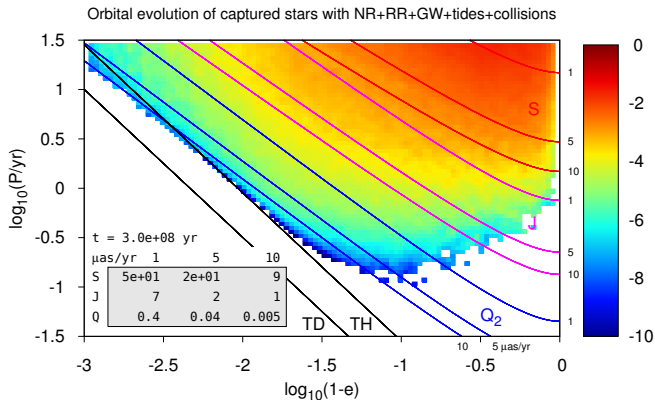
Evolution of tidally-captured relativistic stars in a dark cusp



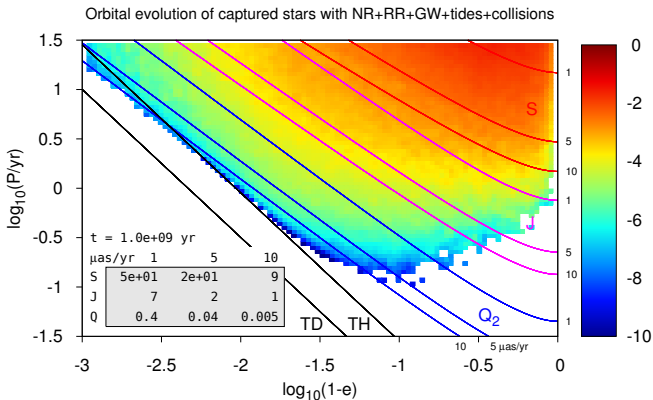
Evolution of tidally-captured relativistic stars in a dark cusp



Evolution of tidally-captured relativistic stars in a dark cusp



Evolution of tidally-captured relativistic stars in a dark cusp



Summary

- ▶ **Theoretical results (more in Ben Bar-Or's talk)**
 - ▶ NR, RR, GW dissipation and secular precession can be treated analytically as effective diffusion with correlated noise.
 - ▶ The steady state depends mostly on NR, which erases AI.
- ▶ **General applications**
 - ▶ Relativistic loss-cone modeling of galactic nuclei in $N_\star \gg 1$ limit.
 - ▶ Plunge / EMRI rates and branching ratios.
- ▶ **Implications for the Galactic Center**
 - ▶ Origin of S-stars: Dark cusp + binary capture favored.
 - ▶ $\mathcal{O}(100)$ captured low-mass relativistic stars may exist in GC, but strongly relativistic orbits suppressed by tidal interaction with MBH.